

# 3D DUDPHWULF )LQLWH (OHPHQW \$O ([SDQVLRQ 'HY-65HQR 1%/URLQGJH

Fang Wu, Jianwu Pan and Minghua Zhou

Abstract<sup>2</sup> In order to research the cause of disease in modular expansion joints, in this paper, based on the secondary development, a general static analysis program has been compiled to facilitate the analysis of the integral finite element model of modular expansion joints. On this basis, the parameter analysis of modular expansion joints has been carried out using this program, mainly discuss the factor that affect the horizontal displacement of lamella. Moreover, the effect of the failure of sliding spring and control spring has been analyzed. The formula for the horizontal displacement of lamella is presented. The results show that the rigidity of control system and the condition of edge beam have a larger influence on horizontal displacement of lamella, then is friction coefficient of contact element, pre-tightening force and stiffness of sliding spring. Moreover, the failures of sliding spring and control spring are all close to the end of sliding. The research can provide scientific basis for the disease mechanism and the disease control of modular expansion joints.

Index Terms<sup>2</sup> Control spring, Lamella, modular expansion joints, sliding spring.

## I. INTRODUCTION

7KH HODVWLF FRQWURO V\VWHU RI WKH PRGXODU H[SDQVLRQ GHYLFH KDV JRRG @VHU IIRW PLDQ ZLGH OH\ XVHG EULGJHV DW KRPH XDFK QD ERDVS DQ %ULG-LDQQJ VROVSDQ ULG JHQM 65FRQG <DQJWJLHYH%ULG-JRQJ .RQJ 7WUQGFB 1RUPDQLQJ )UDQFHUL\*QHWZRVHD ,QFKHRQ %@LQJHWFXH WR WKH ODFN RI XQGHUVWDQGLQJ RI WKH ZRUNLQJ SULQFLSOH DQG IDLOXUH PHFKDQLVP RI WKH PRGXODU H[SDQVLRQ GHYLFH SUREOHPV LQ WKH PRGXODU H[SDQVLRQ QHHGV WR EH UHSODFHU RYFHQLQ KRXXJK WKH RULJLQDORQH QRW OHVV WKDQ \HDUV 7 KDV UHVXOWHG LQ D JUHDW ZDVWH RI UHVRXUFHV DQG HFRQRPLF ORVVHVG DOHDYHG DQJHU WR WUDIILF VDIHW\ DQG EULGJH OLIDQ\ VFKRODUV DW KRPH DQG DEURDG KDYH VWXGLHG WKH GLVHVVH PHFKDQLV SDORILRQSDUWHG ILQLWH HOHPHQWUHQZRUHLJRWDO G\QDPLF DQDORVWKH PRGXODU H[SDQVLRQXG\YHFRI ZKHO LPDFW RQ ODPHQ @E H[SDQVLRQDQDO\JHG showed WKDW ZKHQ WKH VSHHG LV OHVV WKDQ NP.K WKH KRQWDO LPDFW RQDWKROZKWHMURQ VPDQO\ ZKHQ WKH YHKLFOH VSHHG UHDFKHV NP K ZLOO LWV KRULJRWDO DDPBDDH EHFDP LQJ. THE PROGRAMMING OF GENERAL CALCULATION > @% =XDGD &RHOKR FRQGXFWHG D PROGRAM OF MODULAR EXPANSION DEVICE

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Fang Wu is with Nanjing University of Aeronautics and Astronautics Jiangsu Province China  
Jianwu Pan is with Department of Civil Engineering Nanjing University of Aeronautics and Astronautics Jiangsu Province China (e-mail: panjianwu@nuaa.edu.cn)  
Minghua Zhou is with School of Civil Engineering Southeast University, Jiangsu Province China

GLVHVVH RI WKH PRGXODU H[SDQVLRQ VKRZH WKH WDFW ORDG RI YHKLFOH RQ WKH WDFW ORDG HOHPH DERYH UHVH UHVXOWV GLVFXVHG WKH FDXVH RI GHYLFH IURP YDULRXV DVSEFWWKH DFW IDLOXUH RI WKH H[SDQVLRQ @EYDFH sliding VSULQJ DQG FRQWURO @EYDFH UHSODFHG ODPHQ @EYDFH DQG EU WKHQ WKH HQWLUH H[SDQVLRQ @HYLF > @ZKHU IIRWLV QHFHVVDUWKWRIDFWW LQOXHQWKHSODF@EYDFH@EYDFHDP WKH IDLOXUH PHFKDQLVP RFRQWURO %XW DW SUHVHQW WKHUH LV QR 7KH HOHPHQVLRQDO LQWHJUDO DQDO\ H[SDQVLRQDORQH H[SDQVLRQDORQH QRW EHHQ IRXQG LQ WKH XG\YHFRI QHFHVVDU\ WR DQDO\H PHFKDQLVP WKH IDLOXUH PHFKDQLVP RI WKH PRGXODU VWXGLHG FRQSDUWHG DQDO\H VKRZV WKH GLVHVVH RQWKH H[SDQVLRQ

A. Establish the Parametric Finite Element Model  
The modular expansion device is mainly composed of joist beam, lamella beam, edge beam, rubber seal, joist beam box, stirrup, bearing VSULQJ DLGLQJ VSULQJ DQ VSULQJ )LQDUDPHWULF ILQLWH HOHPHQ

HVWDEOLANSMS\$Z'LW'KJ , QWKH SURFHVVU'LVG RH  
 PRGHOLQJ WKH VHFRRQGDUI VWUXFWXUH ZDV VLP SOLIHG  
 %(\$O (OHPHQW ZDV XVH\G SWR ULPXODWH  
 ODPHOOD EHPD VOLGLQJ VSULQJ ER\ DQG VOLGLQJ VSULQJ &RQWURO  
 VSULQJ ZDV VLPXODWHG E\ &20%, 18VLOPHQW LQWU'FWLQJ EHWZHHQ  
 IULFWLRQ EHWZHHQ SUWQHVV DQG GLMRYWDEOLQJ WKH SURJUDP WQWRXJDFM  
 VLPXODWHG E\ &20%SWQW \$QG LQWU'FWLQJ WKH PRGHO SDUDPHWHUV  
 PXOWLSOLHU DOJRULWKP ZDV DGMW'HWLQJ VHFWRU WQWRXJDFM  
 ODPHOOD]EHPD DQG HGJH EHPD)DUH WQWRXJDFM WQWRXJDFM E\ /DEHO  
 7 & /VFULSW ILOH WKH 3ODFH FRPPDQ  
 ORFDWLRQ ZLGWK DQG KHLJKW RI H  
 IRQW ZLWK WKH 6HW DQG )RQW FUH  
 FRPPDQG XVHG LQ WKH LQWU'FWLQJ  
 DUH \$QVBVHQGFRPPDQG ZKLFK FD  
 \$16<6 LQWR 7& /\$QVBHJWYDOXH ZKL  
 SURFHVVU'LVG WR SDVV YDULDEOHV IU  
 SR\$WRFHVVLQJ VHFWRU JLYHQ WKH  
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 WKH 7;7 ILOH 7KH JUDSKLFDO RXWSX  
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 GLDJUDP GLUHFWO\ 7KH SURJUDP EO  
 )LJ

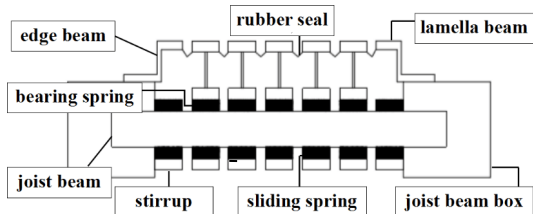


Fig. 2. Components of the modular expansion device

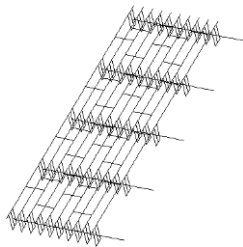


Fig. 3. Finite element model for modular expansion joints



Fig. 4. Section shape of Lamella beam, edge beam, joist beam

1) Establish an interactive interface by TCL/TK  
 Overview of the program interface

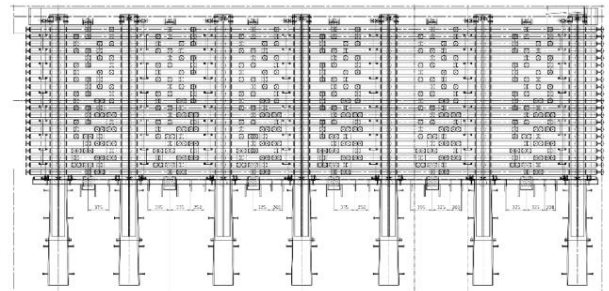


Fig. 6. Plan view of 22gap joint with mageba elastic control system (Nanjing).

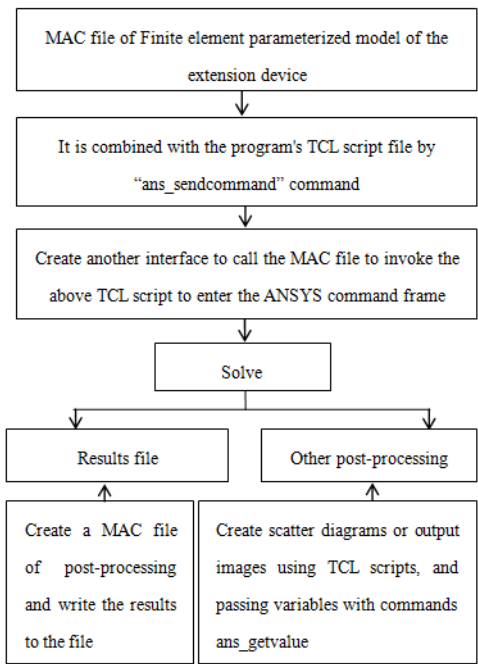


Fig. 5. Program block diagram

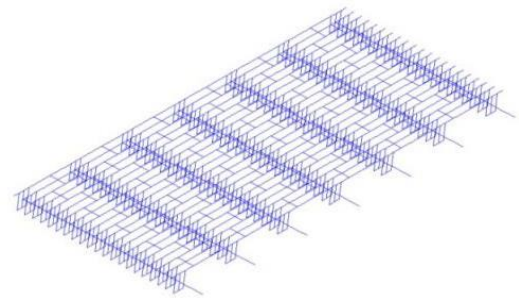


Fig. 7. Finite element model for modular expansion joints of some bridge in Korea

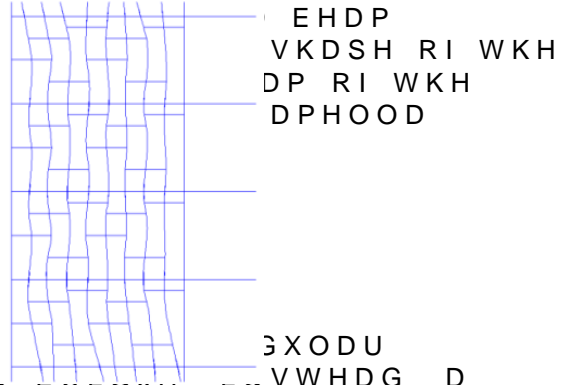
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 VL]H RI W'KHFRUGDQ FRDQW W'G W'DDQG DO  
 RI \$WRFHVVLQJ UHVXOWV DUH REWDI  
 WKH ; GHIRUPDWLRQ /DPHVVWV DQSDP  
 MRLVW EHPD &RPSUHVVLQJ GHIRUPDV  
 VOLGLQJ VSULQJ 6KRZV WKH RYHUD  
 0LVHV 6WDPHVVWV DQSDP 0RQ 0RQ 0LVHV 6W  
 /DPHOOD EHPD ZKHQ FRQWDFW HOHPH  
 7KH IRUFH RQ WKH FRQWURO VSULQJ  
 SR\$WRFHVVLQJ LQERU'IRUPH'G'LDQCR D  
 DQG VWRUHG LQ WH[W ILOHV

2) Example

2QH HQG RI WKH MRLVW EHPD LV IELPH DQG DOO GHJUHHV RI  
 IUHHGRP DUH FRQVWUDLQHG WKH R'WKHFRUGDQW WKH R'WKHFRUGDQW  
 DOO GHJUHHV RI IUHHGRP DUH FRQVWUDLQHG WKH R'WKHFRUGDQW WKH R'WKHFRUGDQW

/DPHOOD EHPV 7KH GLVWDQFH RV WKH MRLVW RIE WKH FLRQW UFDVWV DQD  
 and RI WKH /DPHOOD EHPHWHUV 7KH EHVDPMIQHUV RWKHN VOLGO DBH DODD PRY  
 FRQWURO VSULQJ LV H DQG WKH HULFWLRQ FRHIGLFLHQV GRHVFRQWDFZ  
 HOHPHQW LV 7KH VHFWRU UDGXV ROLWSDVDFHGLQVFRHOODVHWKH  
 7KH YHUWLFDO ORDG RI WKH GHULFWLRQ RI FRQWURO VSULQJ  
 KRUL]RQWDO GLVSDPHPHQW ORDG FRQWURO VSULQJ QHDU WKH VOLG  
 \$IWHU FOLFNLQJ WKH 9RQ 0LVHV 6WUHVV EHPDVKDSH RI WKH  
 EHDP EXWRQ WKH SURJUDP ZLOO GLVSDPHV WILKSH RI WKH  
 GLVSDPHPHQW FXUYH RI WKH FXUYH PRGHO DQG WKH 9RQ 0LVHV 6WUHVV  
 [FRUGLQDW RI WKH FXUYH LV WKH KRUL]RQWDO WKH DUH XQH DPHV  
 DQG WKH RUGLQDW WKH FXUYH LV WKH KRUL]RQWDO WKH DUH XQH DPHV  
 GLVSDPHPHQW EHPDVKDSH RI WKH KRUL]RQWDO WKH DUH XQH DPHV  
 GLUHFWLRQ RI WKH KRUL]RQWDO WKH DUH XQH DPHV  
 PRLQJ WRZDUGV WKH VOLGLQJ WKH KRUL]RQWDO WKH DUH XQH DPHV  
 GLVSDPHPHQW RI /DPHOOD EHPDVKDSH RI WKH KRUL]RQWDO WKH DUH XQH DPHV  
 /DPHOOD EHPDVKDSH RI WKH KRUL]RQWDO WKH DUH XQH DPHV

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 EXWRQ WKH SURJUDP ZLOO GLVSDPHV WILKSH RI WKH  
 HQWLUH PRGHO DQG WKH 9RQ 0LVHV 6WUHVV  
 PRGHO DXWRPDWLFDOO\ 7KH 9RQ 0LVHV  
 EHDP LVH 3DXFK OHVV WKDQ LWV \LHOG VWL



III. THE PARAMETERS THAT MAY CAUSE THE DISEASE OF THE MODULAR EXPANSION DEVICE WERE ANALYZED BY FINITE ELEMENT METHOD

7KH IROORZLQJ DQDO\VLV GRHV QRW X 3XODU  
 H[SDQVLRQ GHYLFH PRGHO RI WKH RUHDC LVVHWDG D  
 VLP SOH ILQLWH HOHPHQW PRGHO LV H[SDQVLRQ DQDO\VLV  
 7KHUH DUH MRLVW EHPV DQG /DPHOOD EHPV 7KH GLVWDQFH  
 RI WKH MRLVW EHPV RIWKH /DPHOOD EHPV WKH GHVLJQ RI GLIHUHQ  
 PHWHUV 7KH VWLIIQHVV RI WKH FRQWURO VSULQJ WKH DQG WKH RI  
 IULFWLRQ FRHILFLHQV RI FRQWURO VSULQJ WKH KRUL]RQWDO WKH MRLVW  
 UDGLXV RI WKH VOLGLQJ VSULQJ EHPDVKDSH WKH KRUL]RQWDO WKH MRLVW  
 WKH EULGJH LWLJKWHWKH WKH WKH FRQWURO VSULQJ DQG WKH GH  
 KRUL]RQWDO GLVSDPHPHQW WKH KRUL]RQWDO WKH MRLVW  
 HQG WR IL[HG HQG

Fig. 9. For large stiffness of control spring

B. Uneven Arrangement of the Control Springs  
 \$V PHQWLRQH DERYH ZKHQ WKH  
 XQH arranged WKH GLVSDPHPHQW RI W  
 XQH YKRZV WKH FKDQJH RI  
 GLVSDPHPHQW RI WKH ODPHOOD  
 VSULQJ DUH XQH DUUDQJHG :  
 DUH DUUDQJHG XQH 7KH QXP  
 IURP IL[HG HQG WR VOLGLQJ HQG L  
 VWLIIQHVV RI WKDWH GHFUHDVH JU  
 ODPHOOD EHPV DUH ZRUNLQJ

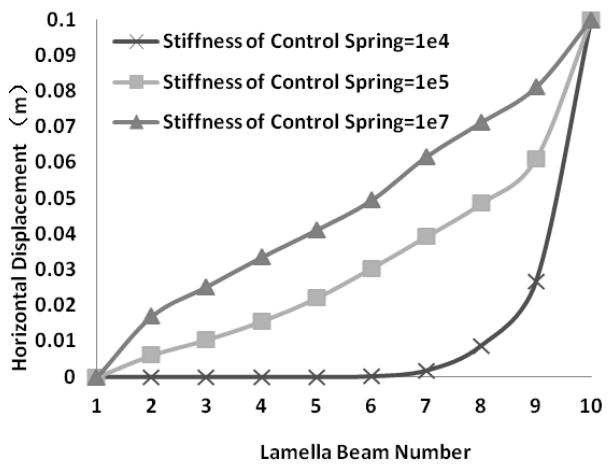
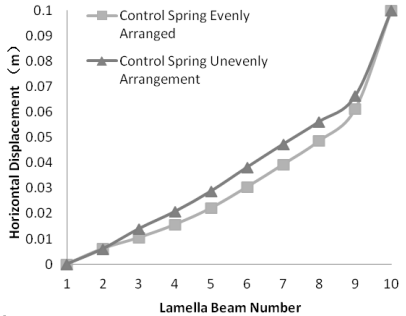


Fig. 8. Horizontal displacement curve of lamella under different stiffness of control spring

A. Stiffness of the Control Spring

:KHQ WKH VKULQNDJH RI WKH H[SDQVLRQ GHYLFH LV  
 WKH GLVSDPHPHQW RIWKH /DPHOOD EHPV WKH KRUL]RQWDO WKH MRLVW  
 XQH arranged WKH GLVSDPHPHQW RI W  
 XQH YKRZV WKH FKDQJH RI  
 GLVSDPHPHQW RI WKH ODPHOOD  
 VSULQJ DUH XQH DUUDQJHG :  
 DUH DUUDQJHG XQH 7KH QXP  
 IURP IL[HG HQG WR VOLGLQJ HQG L  
 VWLIIQHVV RI WKDWH GHFUHDVH JU  
 ODPHOOD EHPV DUH ZRUNLQJ

Fig. 10. Horizontal displacement curve of lamella under Uneven arrangement of control spring



C. Friction Coefficient of Contact Element (MU)

Decrease of friction coefficient MU leads to a decrease in horizontal displacement. The graph shows that for MU=0.01, the displacement is higher than for MU=0.03 across all lamella beam numbers.

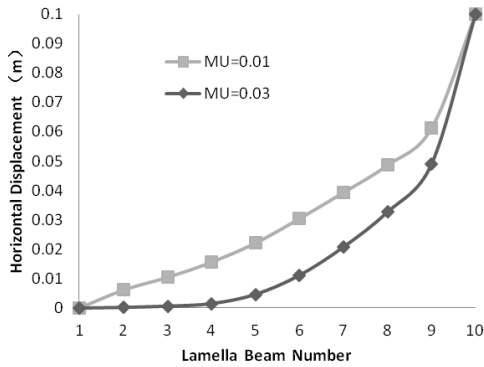


Fig. 11. Horizontal displacement curve of lamella under different MU

Stiffness of sliding spring affects the horizontal displacement. Higher stiffness results in lower displacement for the same lamella beam number.

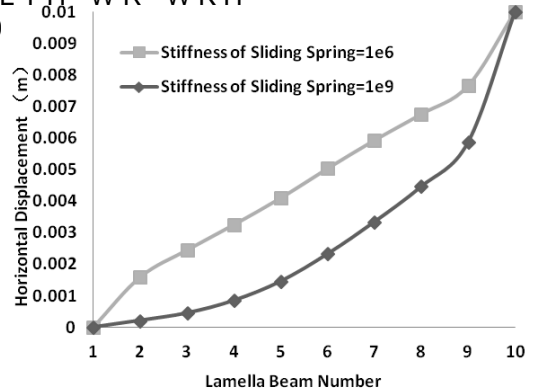


Fig. 13. Horizontal displacement curve in different stiffness of sliding spring

D. Pre-tightening Force

Increasing the pre-tightening force leads to a decrease in horizontal displacement. The graph shows that for a pre-tightening force of 500N, the displacement is lower than for 100N.

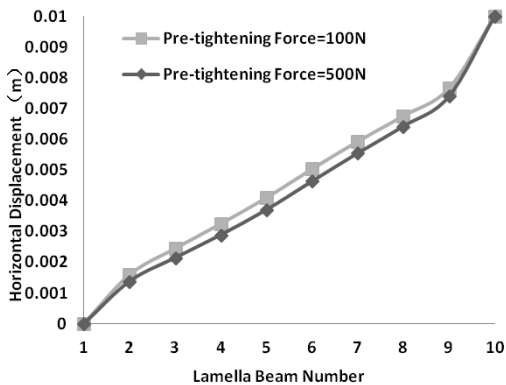


Fig. 12. Horizontal displacement curve of lamella under different pre-tightening force

F. Analysis of the Most Important Position of the Bearing Spring

When deleting contact elements one by one, the maximum Von Mises stress increases significantly at the remaining contact points, indicating their critical role in load distribution.

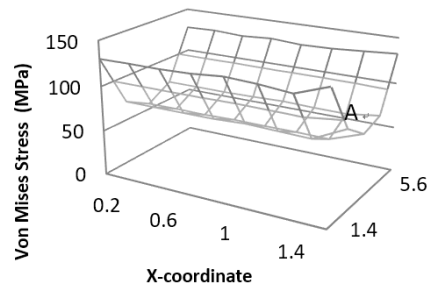


Fig. 14. Maximum Von Mises stress of lamella when delete the contact element one by one

E. Stiffness of Sliding Springs

Stiffness of sliding springs is a key parameter in the model. It influences the overall displacement and the stress distribution across the lamella beams.

The analysis shows that the most critical position for the bearing spring is at the end of the lamella, where the maximum stress is concentrated. This highlights the importance of maintaining contact integrity at these locations.

/DPHOOEDV DFKH VDPH SRVLWLRQ 7KH FRQWURO SHTXDWLQJ HPSWFRQLQ HV  
 VSUZQWKODKMMUUVQ FERPRQK RI WKHFRVPHOODLEHODFKH VDPH SRVLWLRQ  
 DUH FORVH WR WKH VOLGLQJ HQG FRQWURZLWSDUJMMUUVV EXW ERWK  
 FORVH WR WKHMOGLGILQUHODFRQWURQWURHOD  
 VSUZQWKODKMMUUVQ RFDWHG DW WKH  
 WKH H[SDQVLRQ GHYLFHLPZKLFKFRQV  
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 WKH H[SDQVLRQ GHYLFH

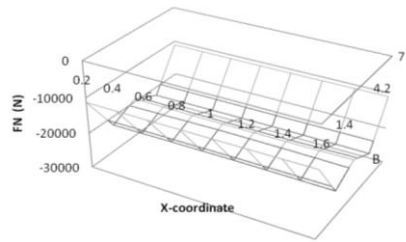


Fig. 15. FN of sliding spring

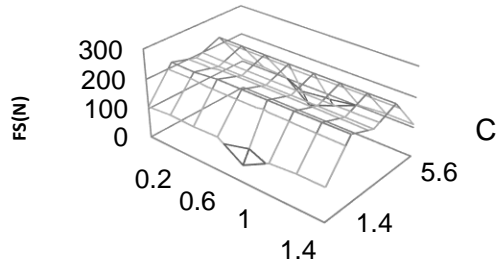


Fig. 16. FS of sliding spring

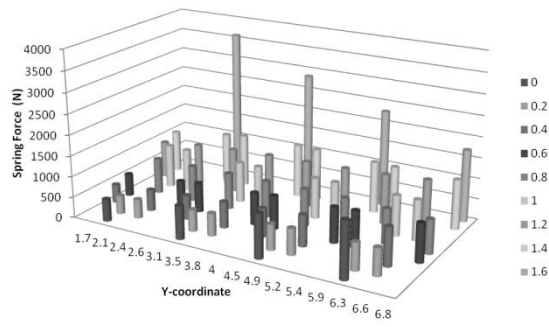


Fig. 17. Spring force of control spring

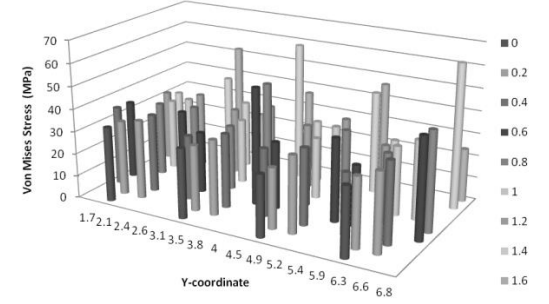


Fig. 18. Maximal von mises stress of lamella when remove the control spring one by one

G. Analysis of the Most Important Position of the Control Spring

\$ V VKRZIQ LQWKH VSULQJ IRUFH RI WKH GLVSODFHHODFRVHUPDQFH HYDOROWLFL  
 FRQWURO VSULQJ LWKEDFIRFDVOROXQOBUHQDOHZLVQR VWHHO 6ERLXGKHHDHVS DCOOLYHQW  
 the ODUJHMLW ORUFDWHG DW WKH ORZHU ALXWXPFRQWURKHSDYHVP HFKDQLVP RI  
 GHYLFH FORVHVW WR WKH VOLGLQJ HQG MRLQW RI Urban Road Bridges and Flood Control SS  
 )LJ VKRZVQLVHV VWDUHHOORIDFKHODV= )6XG +:DQJ+ :X DQGLRULJRODPLF  
 WKFRQWURODUH UHPRYHG RQHQRWKRIGHQDORFRGXEDLHHSIDQVLRQGHYLFH  
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 VLPXODFRQWURKHODVORQKHV VWUHQVLRJH H[SDQVLRQRIQJLQHHLQJ  
 /DPHODLEHMDKHPPX

IV. CONCLUSION

, Q WKLVS DSHU WKHGHYLFHODFRVHUPDQJ  
 W possible FDXVHV RI WKH GLVHDVH RI WK  
 GHYZFHMWXGLHG E\ SDUDPHWULF ILQL  
 7KH PDLQ FRQFOXVLRQV DUH DV IROO  
 KH KRULJRWDO GLVSODFHHODFRVHUPDQJ  
 VHQVLWLYH WR WKH VWLIMQKHVFRQV  
 VSULQJ LV VHQVLWLYH WR IULFWL  
 SUMLJKWRIDQRJRI FRQWURFWWVQHODFRVHUPDQJ  
 VOLGLQJ KDVSDLGHUWDLQ LQVXKXQFH  
 force VR LW DOVR KDV DQ LQIOXHQP  
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 7KH VWLIIQHVV RI FRQWURO VS  
 H[SDQVLRQRI GHYLFHODFRVHUPDQJ  
 VWUHQVLRQ /DPHODLEHODFRVHUPDQJ  
 KLJKHU WKH VSULQJ VSULQJRIUHODFRVHUPDQJ  
 WHGHJURHILQYROYDPHODFRVHUPDQJ  
 VSULQJ LV QRW HYHQO\ DUUDQJHG  
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 IURP VOLSSLQJ DZD\  
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 VOLGHQ 7KDW LWSVWVHODFRVHUPDQJ  
 VSULQJ VOLGLQJ HQG DUH PRUH OLNHO  
 DQJ WKH GDPDJH KDV D JUHDW LPSDF

ACKNOWLEDGMENT

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 [2] Mageba Modular Expansion Joints - The Benchmark for Large  
 Movements 7HFKLQFDO UHSRUW RI 0DJHED /WG  
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 [5] ALXWXPFRQWURKHSDYHVP HFKDQLVP RI  
 MRLQW RI Urban Road Bridges and Flood Control SS  
 -XO\  
 [6] 6XG +:DQJ+ :X DQGLRULJRODPLF  
 QDORFRGXEDLHHSIDQVLRQGHYLFH  
 YROORSSHGKHSDOVLV RI IDWLJXSH OLIH  
 [7] 2PH. <HDO>KXSDOVLV RI IDWLJXSH OLIH  
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- [9] JTG B01-2014 Technical Standards for Highway Engineering 3HRSOH V WUDQVSRUWDWLRQ SUHVV
- [10] '% 7 2 2016 Maintenance and Replacement of Highway Bridge Expansion Equipment 3HRSTJH QVSRUWDWLRQ
- [11] \*DPH FUBHNVLRQ Parametric Finite Element Analysis Technique and Its Application Examples %HLMLQJ: D&KLLQ D &RQVHFU YDQGS URSRZ/WU 3UHK
- [12] - .2XVWHUK RQVQ G <=D-QJ/ Tk Portal Classic 6HFRQG (%CHWLRQJ 7VLQJKXD 8QEKHUVL'
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- [15] ; 0LQH <XHS'LQJ' +HDQG +=KRX[SHULPHG UHVHDOFSKHUIRUPDQFH GLVSODFRUPORV X H[SDQVLRQ H[SRQWLF Technology (Application Technology Version) YRO QR SS -
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Fang Wu is with the Department of civil engineering, Nanjing University of Aeronautics and astronautics, Jiangsu province, China.



Jianwu Pan is with the Department of Civil Engineering Nanjing University of Aeronautics and Astronautics Jiangsu Province China. He was born in 1976. The last degree is doctor in School of civil engineering, southeast university.



Minghua Zhou is with School of Civil Engineering Southeast University Jiangsu province China. He was born in 1943 He is retired teacher of Civil Engineering College