

Modeling and Optimization of Milling Process by using RSM and ANN Methods

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Abstract— Nowadays numerical and Artificial Neural Networks (ANN) methods are widely used for both modeling and optimizing the performance of the manufacturing technologies. Optimum machining parameters are of great concern in manufacturing environments, where economy of machining operation plays a key role in competitiveness in the market.

In this paper, the selection of optimal machining parameters (i.e., spindle speed, depth of cut and feed rate) for face milling operations was investigated in order to minimize the surface roughness and to maximize the material removal rate. Effects of selected parameters on process variables (i.e., surface roughness and material removal rate) were investigated using Response Surface Methodology (RSM) and artificial neural networks. Optimum machining parameters were carried out using RSM and compared to the experimental results. The obtained results indicate the appropriate ability of RSM and ANN methods for milling process modeling and optimization.

Index Terms: Milling operations, Optimization, Modeling, Response Surface Methodology, Artificial Neural Network

I. INTRODUCTION

The selection of efficient machining parameters is of great concern in manufacturing industries, where economy of machining operations plays a key role in the competitive market. Many researchers have dealt with the optimization of machining parameters.

The RSM is a dynamic and foremost important tool of Design of Experiment (DOE) where in the relationship between process output(s) and its input decision variables, it is mapped to achieve the objective of maximization or minimization of the output properties. RSM was successfully applied for prediction and optimization of cutting parameters [1,2]. M.S. Shunmugam et al, investigated selection of optimal conditions in multi-pass face-milling using a genetic algorithm [1]. Dae Kyun Baek et al, investigated optimization of feed rate in a face milling operation using a surface roughness model [4]. Prediction of surface roughness in CNC face milling using neural networks and Taguchi's design of experiments were investigated by P.G. Benardos et al[5]. Jae-Seob Kwak used Taguchi and RSM for geometric error in surface grinding process [6]. The influence of feed rate and cutting speed on cutting forces, surface roughness and tool-chip contact length during face milling were investigated by I. Korkut et al. [7]. Multidisciplinary optimization of a car component under NVH and weight constraints using RSM was investigated by M. Azadi et al. [8].

In this study, based on experimental data in milling process,

Response surface methodology and artificial neural network were employed to develop prediction models for surface roughness (R_a) and material removal rate (MRR). Then, the results were compared. Response surface methodology is used to find the optimal cutting parameters. To evaluate the accuracy of results, several experiments were conducted and obtained results were investigated.

II. EXPERIMENTAL PROCEDURES

To investigate how process parameters affect on process state variables (i.e., R_a and MRR), several experiments were conducted. A central composite design including three levels of factors for finishing and rough machining operations was used. The feed rate, spindle speed and depth of cut considered as independent input variables. Linear and second order polynomials were fitted to the experimental data for obtaining the regression equations. The lack of fit test, variance test and other adequacy measures were used in selecting optimum models.

The experiments have been carried out on a Hurco 5HP CNC vertical milling center equipped with a ϕ 60 mm four-flute face-milling cutter with grade 1C28M40 inserts. The workpiece material used in these tests was 6061-T6 Aluminum. Table 1 shows milling machine input variables and experiment levels.

All specimens in this experiment were conducted using Sunoco Sunicut 151 cutting fluid.

TABLE 1: PROCESS VARIABLE AND EXPERIMENTAL LEVELS

Process parameters			
Milling operations	Feed rate, F, (mm/min)	Spindle speed, S, (rpm)	Depth D, (mm)
Finishing	500	4000	0.25
	1000	6000	0.5
	2000	8000	1
Roughing	3000	4000	2
	4250	6000	3
	5500	8000	4

III. PROCESS MODELING AND DISCUSSION

Once the cutting operations are accomplished, the surface roughness, R_a , is measured. R_a was measured using a portable Mitutoyo Surftest Profilometer with a roughness cut-off of 0.8 mm. Material removal rate calculated with equation 1. The experimental results for finishing and rough machining are shown in Table 2.

$$MRR = F \times d \times D \quad (1)$$

where F , d and D are respectively the feed rate, the depth of cut and the tool diameter.

In this section, by using RSM and ANN methods, the analysis of experimental results which obtained during rough machining and finishing are carried out and the results are compared.

A. Modeling by Using Rsm

By using "T" test, significance of each parameter effects and their interactions on the process were studied. Response surface method was used to fit linear and second order polynomials on experimental data [9].

TABLE 2: EXPERIMENTAL RESULTS

Finishing cut						Roughing cut					
Test	Cutting parameters			Measured variables		Test	Cutting parameters			Measured variables	
	Feed rate (mm/min)	Speed (rpm)	Depth (mm)	R_a (μm)	MRR (mm^3/min)		Feed rate (mm/min)	Speed (rpm)	Depth (mm)	R_a (μm)	MRR (mm^3/min)
1	1000	8000	0.5	0.17	30000	1	4250	8000	3	0.36	765000
2	500	8000	1	0.1	30000	2	3000	8000	4	0.26	720000
3	1000	6000	0.25	0.14	15000	3	4250	6000	2	0.25	510000
4	1000	6000	1	0.16	60000	4	4250	6000	4	0.49	1020000
5	500	4000	0.25	0.13	7500	5	3000	4000	2	0.54	360000
6	2000	4000	0.25	0.31	30000	6	5500	4000	2	1.20	660000
7	1000	4000	0.5	0.20	30000	7	4250	4000	3	0.43	765000
8	500	4000	1	0.21	30000	8	3000	4000	4	0.58	720000
9	500	6000	0.5	0.19	15000	9	3000	6000	3	0.40	540000
10	1000	6000	0.5	0.16	30000	10	4250	6000	3	0.43	765000
11	2000	6000	0.5	0.24	60000	11	5500	6000	3	0.67	990000
12	2000	4000	1	0.30	120000	12	5500	4000	4	1.04	1320000
13	2000	8000	0.25	0.24	30000	13	5500	8000	2	0.35	660000
14	2000	8000	1	0.23	120000	14	5500	8000	4	0.45	1320000
15	500	8000	0.25	0.13	7500	15	3000	8000	2	0.24	360000

1) Rough machining case

Considering surface roughness model, statistical analysis shows that the spindle speed and feed rate are the significant model terms. Fig. 1a shows that the increased speed and decreased feed rate lead to decrease R_a . Also, statistical analysis for MRR model indicates the feed rate, depth of cut and interaction of them are significant factors. Fig. 2a indicates that the increased depth of cut and feed rate result in increase MRR.

The final developed models in terms of significant coded factors are shown below:

$$Ra = 0.5127 + 0.6190 F - 0.02130 S \quad (2)$$

$$MRR = 765000 + 225000 \times F + 225000 \times D + 75000 \times F \times D \quad (3)$$

2) Finishing case

Fig. 3a shows the effect of process parameters on the R_a . Statistical analysis for MRR model shows that the feed rate, depth of cut, second order effect of feed rate, second order effect of depth of cut and the interaction of feed rate and depth of cut are the most important terms of the obtained model. Fig. 4a shows that the increased feed rate and depth of cut result in an increase in the MRR.

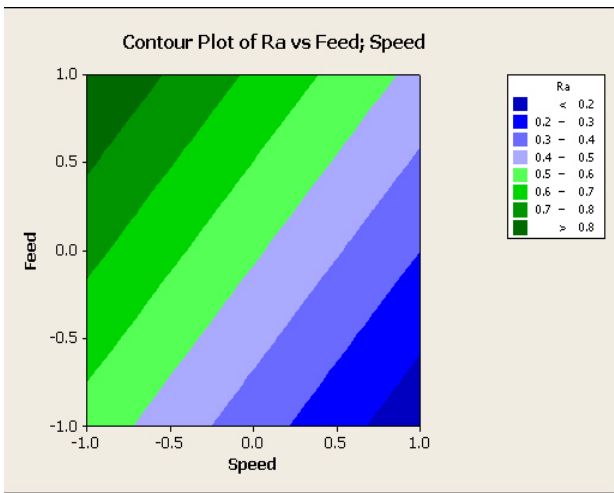
The final developed models in terms of significant coded factors are shown below:

$$Ra = 0.19400 + 0.5600 F - 0.02800 S \quad (4)$$

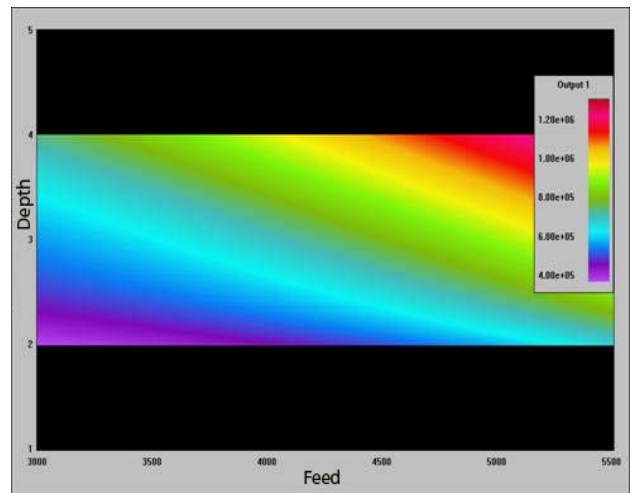
$$MRR = 29571 + 27000 \times F + 27000 \times D + 8571 \times F^2 + 8571 \times D^2 + 16875 \times F \times D \quad (5)$$

3) Validation of proposed models

Figs 5 and 6 show the residual distribution diagrams for finishing and rough machining. The residuals are distributed around normal line. Therefore, the developed mathematical models are appropriate models for predicting and investigating parameters effect.

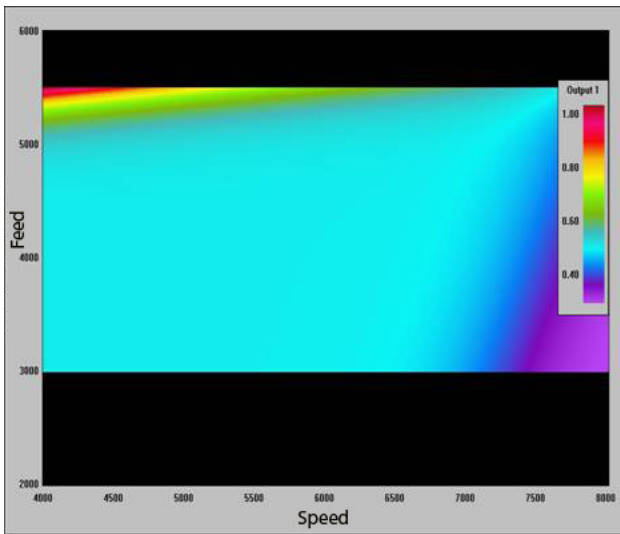


a)



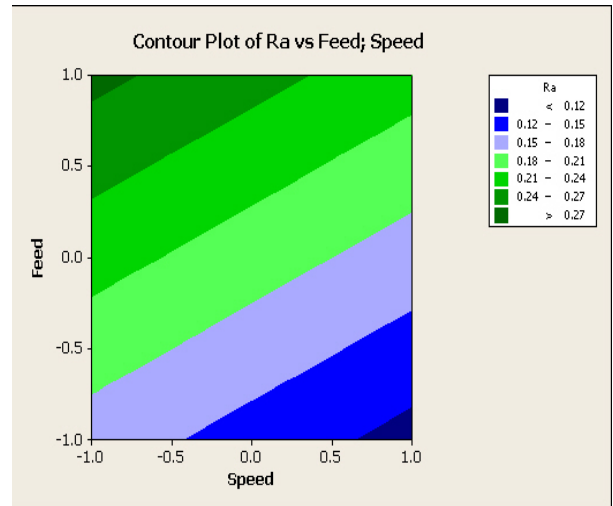
b)

Fig. 2: Effects of feed rate and depth of cut on the MRR (rough machining). a) via RSM, b) via ANN

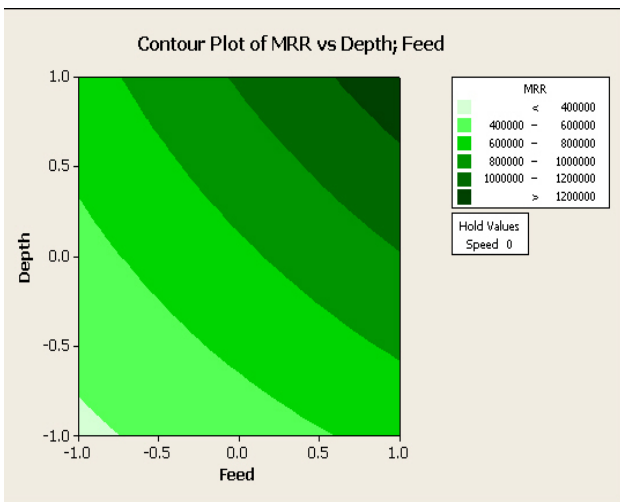


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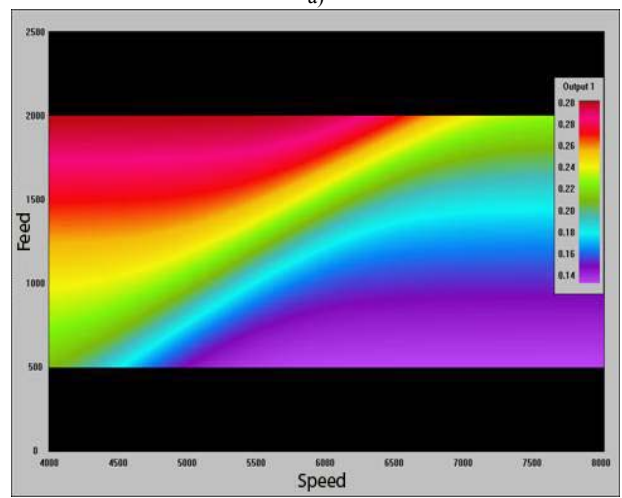
Fig. 1: Effects of feed rate and speed on the R_a (rough machining). a) via RSM, b) via ANN



a)

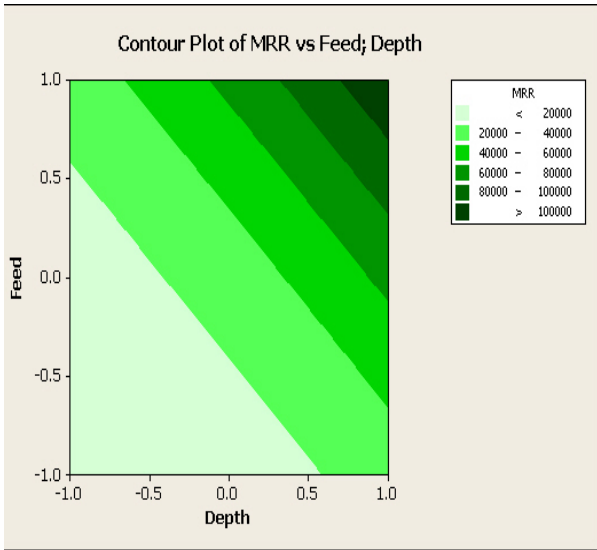


a)

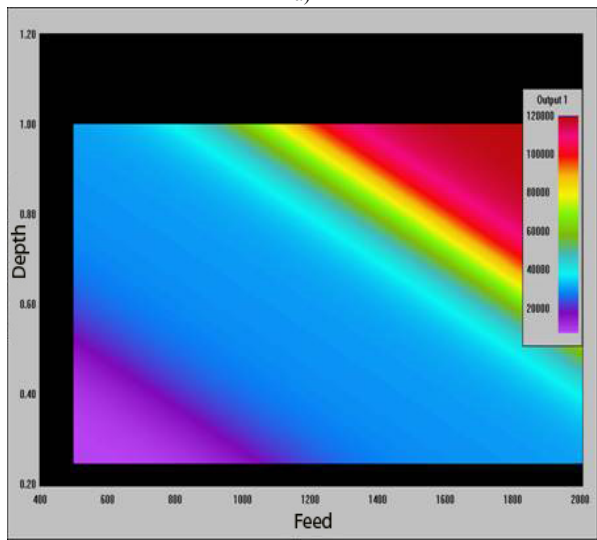


b)

Fig. 3: Effects of feed rate and speed on the R_a (finishing). a) via RSM, b) via ANN



a)



b)

Fig. 4: Effects of feed rate and depth of cut on the MRR (finishing). a) via RSM, b) via ANN

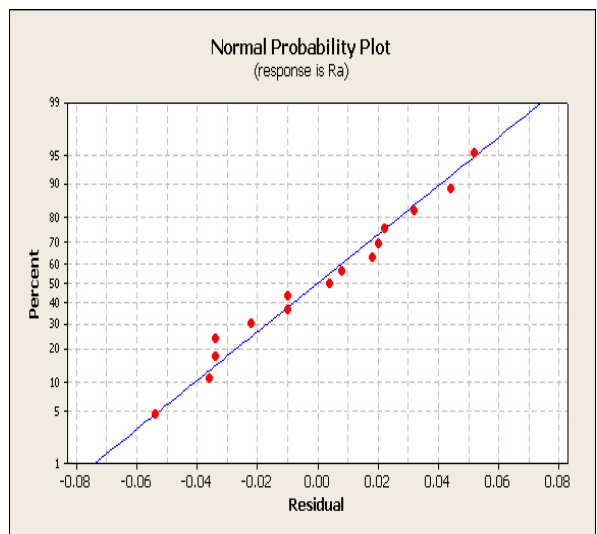


Fig. 5- a: Residual distribution of Ra (finishing)

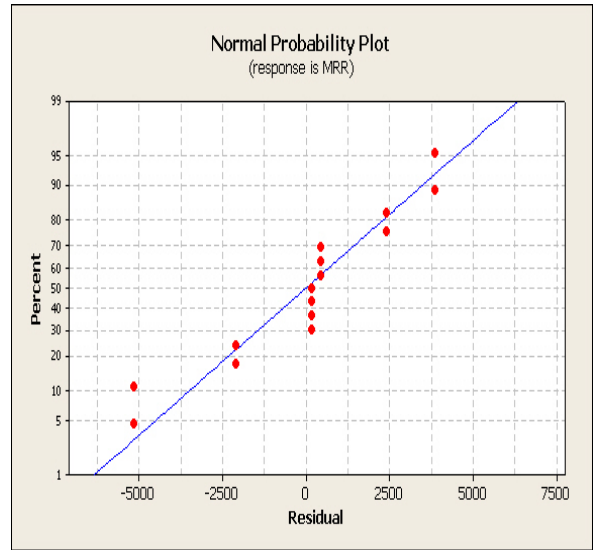


Fig. 5-b: Residual distribution of MRR (finishing)

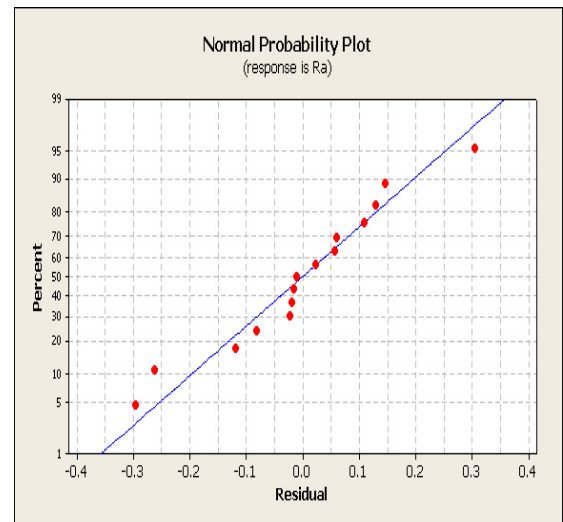


Fig. 6-a: Residual distribution of Ra (rough machining)

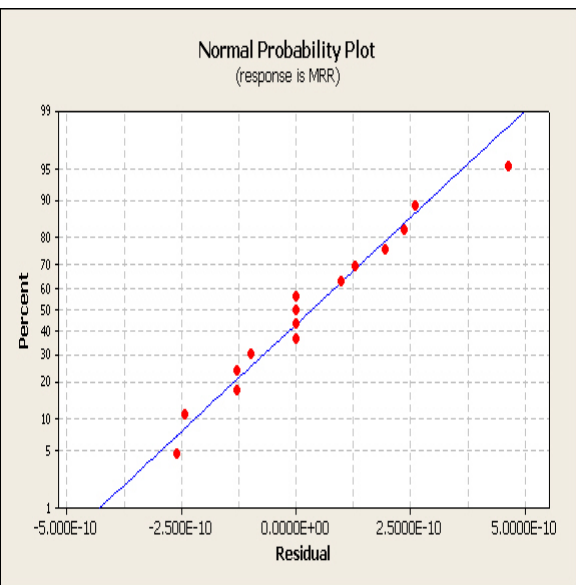


Fig. 6-b: Residual distribution of MRR (rough machining)

B. Modeling by Using Ann

Neural networks are one of the most proper tools in artificial intelligence which are widely used in industry applications. Fifteen experimental data are used for modeling. The feed rate, speed and depth of cut were three parameters considered as network inputs. To have an accurate and reliable model, surface roughness and material removal rate are separately estimated by using a Perceptron neural network. Several network architectures, which are not presented in this study, are tested. The appropriate architecture with one hidden layer is selected, $3 \times 2 \times 1$. Results are presented and discussed in the following sections.

1) *Rough machining case*

The obtained results of ANN for R_a model are shown in Fig. 1b. An increase in speed and a decrease in feed rate lead to a decrease in R_a . As shown in Fig. 2b, the MRR is increased by multiplying the values of feed rate and depth of cut.

2) *Finishing case*

Fig. 3b shows the effects of process parameters on the R_a . The obtained results of ANN for the MRR are shown in Fig. 4b. Results indicate that an increase in the depth of cut and feed rate leads to an increase in the MRR.

3) *Validation of proposed models*

Many tools are available for testing the modeling capacity. In this study, Targets/Network outputs plot are used for checking the performance of the proposed models. Figs 7 and 8 show Targets/Network outputs plot of the proposed neural models, (i.e., the material removal rate and surface roughness).

As shown in Figs 7 and 8, the residuals are appropriately distributed around "X=Y" line. The closer the points fall to the "X=Y" line, the stronger the model. The results of RSM are very like to those of ANN. However, the data coverage of the proposed ANN is more. It indicates the better accuracy of the proposed neural model than the RSM one. The results are presented in Table 3.

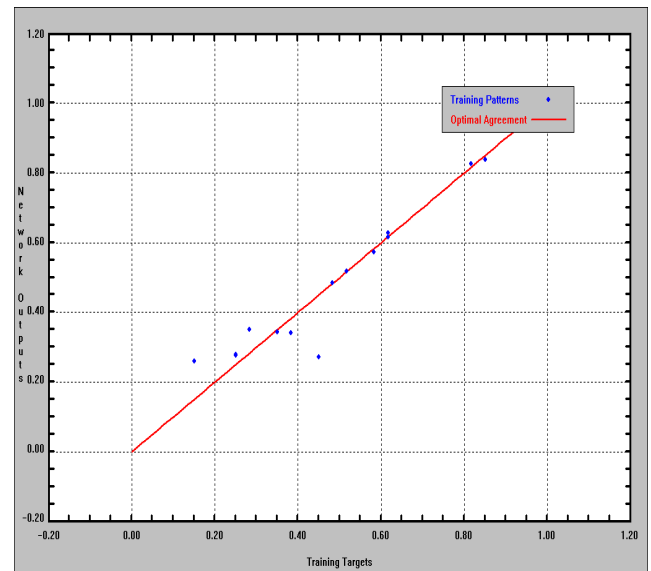


Fig.7-b: Targets/Network Outputs plot of MRR (finishing)

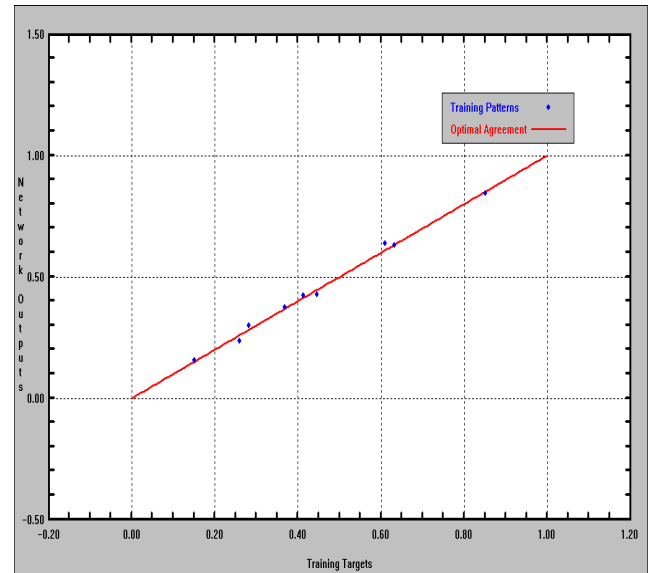


Fig.8-a: Targets/Network Outputs plot of Ra (rough machining)

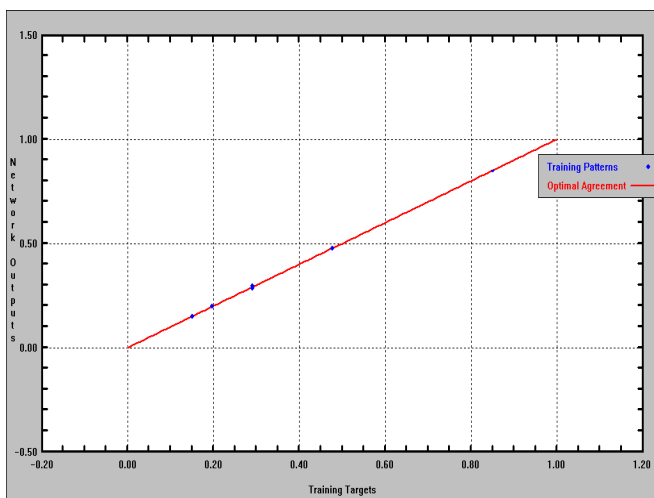


Fig.7-a: Targets/Network Outputs plot of Ra (finishing)

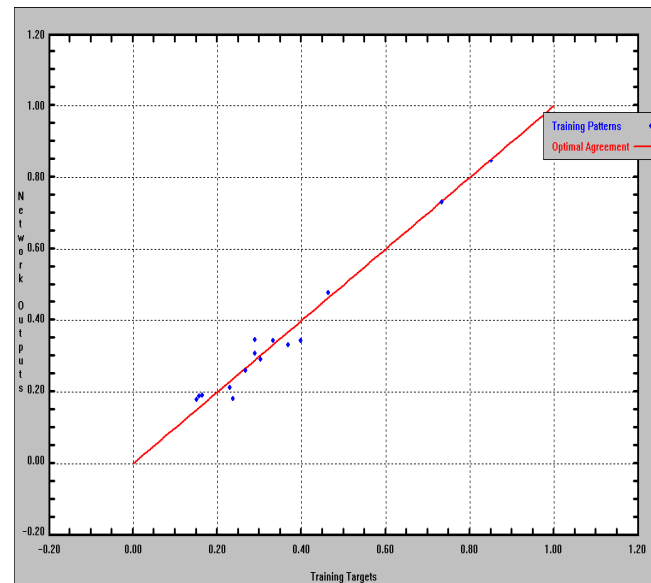


Fig.8-b: Targets/Network Outputs plot of MRR (rough machining)

TABLE 3: EVALUATION RESULTS

Milling operations	Model	RSM	ANN
Finishing case	R _a	73.46%	95.46%
	MRR	99.41%	99.98%
Rough machining case	R _a	69.20%	98.74%
	MRR	99.18%	99.76%
Average error		85.31%	97.73%

corresponding state variables are shown in Table 4.

Furthermore, to evaluate the modeling capacity of the proposed models, several experiments were conducted.

Table 5 shows the experimental data and the validation test. The obtained results have shown the appropriate ability of the RSM for process optimization.

TABLE 5: OBTAINED OPTIMIZATION VALUES OF RSM

Operation	Experimental data	Estimated data with RSM	Error (%)
Rough machining case	R _a =1.04 MRR=132×10 ⁴	R _a =0.8947 MRR=132×10 ⁴	14 0
Finishing case	R _a =0.11 MRR=30000	R _a =0.11 MRR=29800	0 0.6

IV. PROCESS OPTIMIZATION

Response surface methodology indicates areas in the design region where the process is likely to give desirable results. Simultaneous consideration of multiple responses involves first building an appropriate response surface model for each response and then trying to find a set of operating conditions that in some sense optimizes all response or at least keeps them in desired ranges [10].

In this study, process optimization was carried out for both rough machining and finishing simultaneously by using RSM method. Then, the obtained results were evaluated experimentally.

A. Rough Machining Case

In optimization of rough machining case, the material removal rate is attended more than surface roughness. Fig. 9a shows optimum parameters as coded. The maximum material removal rate (up to 1320000 mm³/min) and the surface roughness equal 0.89 μm are obtained with 99% confidence coefficient (see Table 4).

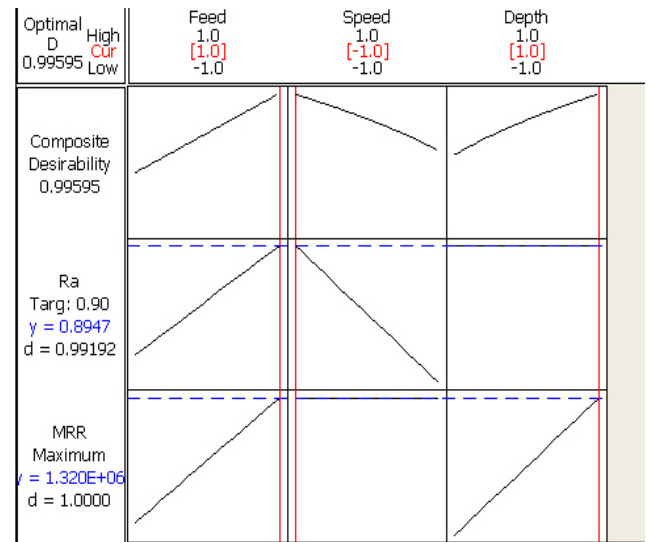
TABLE 4: OBTAINED OPTIMIZATION VALUES OF RSM

Operation	Feed rate (mm/min)	Speed (rpm)	Depth (mm)	R _a (μm)	MRR (mm ³ /min)
Rough machining case	5000	4000	4	0.89	1320000
Finishing case	500	8000	1	0.11	29800

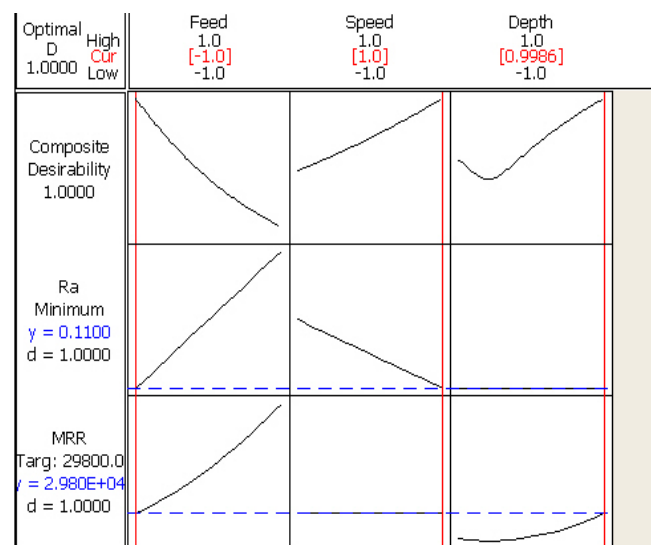
B. Finishing Case

For minimizing surface roughness, R_a is considered to be more important than MRR. Fig. 9b shows optimum parameters as coded.

The optimum machining parameters and the



a)



b)

Fig. 9: Optimization parameters (coded) a) Rough machining case, b) Finishing case

V. CONCLUSION

Based on the conducted experiments and accomplished analysis, the following conclusions can be made:

- 1) The speed and feed rate are the most significant factors in surface roughness model.
- 2) The depth of cut and feed rate and their interaction are significant factors in the material removal rate model.
- 3) The MLP network and RSM provide a very good process modeling. In addition, the former provided the better data coverage value.
- 4) The excellent accuracy (nearly null error) of the RSM optimization procedure is observed during rough machining and finishing.

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