LSCMA Blind Adaptive Algorithm with Comparison of Optimization Capabilities for Smart Antenna Systems

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Abstract—In the present paper convergence characteristics of blind beam-forming algorithm Least Square Constant Modulus Algorithm (LSCMA) are analyzed. This algorithm is used with Smart antenna systems (SAS) for improving the performance of wireless communication system by optimizing the radiation pattern according to the signal environment. This can increase the coverage and capacity of a system in multipath channels by overcoming the interference and noise. The data rate can be enhanced by mitigating fading due to cancellation of multipath components. In this paper optimization capabilities of LSCMA are considered by changing of parameters. The results reveal improvement in gain and reduction in side-lobe level.

Index Terms—Angle of arrival, Array Factor, LSCMA, Multipath, Smart Antenna Systems.

I. INTRODUCTION

An important challenge in Wireless digital communication system is the identification of desired signal from a set of signals available in faded channel. For this SAS are deployed with certain beam-forming algorithms with the property of spatial filtering to differentiate between desired and interfering signals. They are having the potential to reduce noise, to increase signal to noise ratio and enhance system capacity [1, 2]. The constant modulus (CM) criterion is the most widespread blind channel equalization technique based on the principle of restoring the CM property of the incoming signals [3, 4].

CMA can be applied to any signal that has nearly a constant envelope (for example FM, FSK and PSK signals). The incoming signals are multiplied by a set of weights which are calculated by using objective function which is inversely related to the quality of signal. The blind algorithm does not uses any reference signal for extracting the channel information to adjusts the weights. The blind technique without initial training sequence can save the bandwidth and improve the communication efficiency [5].

Many adaptive beam-forming algorithms (ABFA) are based on minimizing the objective function based on error between a reference signal $d(k)$ and the array output $y(k)$.

The reference signal is basically a training sequence used to train the adaptive antenna array or a desired signal based upon an a priori knowledge of nature of the arriving signals. In case where a reference signal is not available one must opt to a group of optimization techniques that are blind to the exact content of the incoming signals.

In this paper the comparison of optimization capabilities of LSCMA blind adaptive BFA with reference to number of antenna elements and their spacing is presented. Section II presents functioning of ABFA and the mathematical description of LSCMA. In section III simulation results using MATLAB 7.0 with reference to number of antenna elements, inter-element distance and angle of arrival (AOA) are obtained to find the optimized values. The array factor plots and LSCMA output for the same values of above parameters are presented.

II. LSCMA ABFA

The method referred as the LSCMA algorithm [6] is also known as an autoregressive estimator based on a least squares minimization [7]. LSCMA overcomes the severe disadvantage of Godard CMA which is slow convergence time. The slow convergence creates a problem in fast varying environments in tracking the signals as well as rapidly changing channel conditions. LSCMA developed by Agee [8] is faster as compared to Godard CMA as it is based on nonlinear least square minimization. Here the cost function is weighted sum of error squares or total error energy. Figure 1 shows ABFA system using LSCMA in which the complex weights $w_1, w_2, \ldots, w_M$ are adjusted by minimizing a certain cost function. LSCMA compensates for the multipath signals whose constant envelope property is lost due to multipath fading, noise and interference. LSCMA has been introduced as an adaptive FIR filter for phase-modulated signals, and studied and applied to array antennas as a narrow-band adaptive beam-former to recover a constant-modulus signal [9].

In fact, the LSCMA algorithm works on the principle that the amplitude of a signal transmitted at CM and received by the array antenna should remain constant [10]. Hence, the main aim of an adaptive beam-forming based on LSCMA is to restore the average of the antenna array output $y(k)$, to a CM as illustrated in Fig. 1. Here the cost function is defined as [11]

$$F(w) = \sum_{k=1}^{M} |p_k(w)|^2 \leq |\Phi(w)|^2$$

(1)
LSCMA is derived by applying “(7)” to the CM cost function [12]

$$F(w) = \sum_{k=1}^{K} \left| \| y(k) \| - 1 \right|^2$$

$$= \sum_{k=1}^{K} \left| w^H x(k) \right|^2$$  \hspace{1cm} (8)

where $y(k) = w^H x(k)$ is array output at time $k$. Comparing “(8)” with “(1)”

$$\Phi_k(w) = \left| y(k) \right| - 1$$

$$= \left| w^H x(k) \right| - 1$$  \hspace{1cm} (9)

Putting “(9)” into “(2)”, one can obtain

$$\Phi(k) = \begin{bmatrix} \left| y(1) \right| - 1 \\ \left| y(2) \right| - 1 \\ \vdots \\ \left| y(K) \right| - 1 \end{bmatrix}$$  \hspace{1cm} (10)

The gradient vector of $\Phi_k(w)$ is given by

$$\nabla \Phi_k(w) = \frac{\partial \Phi_k(w)}{\partial w}$$

$$= x(k) \frac{y^*(k)}{|y(k)|}$$  \hspace{1cm} (11)

Putting “(11)” into “(4)” $D(w)$ can be expressed as

$$D(w) = [\nabla \Phi_1(w), \nabla \Phi_2(w), \ldots, \nabla \Phi_K(w)]$$

$$= \begin{bmatrix} x(1) & y^*(1) & x(2) & y^*(2) & \cdots & x(K) & y^*(K) \\ \end{bmatrix}$$

$$= XY_{CM}$$  \hspace{1cm} (12)

where

$$X = [x(1), x(2), \ldots, x(K)]$$

and

$$Y_{CM} = \begin{bmatrix} y^*(1) & 0 & \cdots & 0 \\ 0 & y^*(2) & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & y^*(K) \end{bmatrix} Y_{CM}^H X^H$$  \hspace{1cm} (13)

Using “(12)” and “(10)” we can write

$$D w D^H w = XY_{CM}^H X^H$$

$$= XX^H$$  \hspace{1cm} (14)

where $m$ denotes the iteration number. The new updated weight vector is the previous weight vector updated by $\Delta$. The
where

\[
D(w)\Phi(w) = X Y_{cm} \begin{bmatrix}
[\gamma(1)]^{-1} \\
[\gamma(2)]^{-1} \\
[\gamma(K)]^{-1}
\end{bmatrix} = X \begin{bmatrix}
y^{\prime}(1) - y^{\prime}(1) \\
y^{\prime}(2) - y^{\prime}(2) \\
y^{\prime}(K) - y^{\prime}(K)
\end{bmatrix}
\]

Thus the algorithm iterates through \( m \) values until convergence. The initial weights \( w(1) \) are to be chosen. The complex-limited output data vector \( r^{\prime}(1) \) is calculated and then \( w(2) \) is calculated. This iteration continues until satisfactory convergence is achieved.

III. SIMULATION RESULTS AND DISCUSSIONS

Simulation of LSCMA adaptive algorithm for antenna arrays using 5, 8 and 10 elements separated by 0.125\( \lambda \), 0.252\( \lambda \) and 0.54\( \lambda \) is performed in MATLAB 7.0. The channel is assumed to be frequency selective. Here it is assumed that the CM signal is arriving at the receiver via a direct path at 45°. The direct path is assumed to be a 32 bit sequence with chip values \( \pm 1 \) and sampling period 4 times per chip. The block length \( K \) is assumed to be 32. The multipath signal is arriving at -30° and is 30% of direct path signal amplitude. Due to the effect of multipath the delays in the binary sequence causes dispersion implemented by zero padding. The direct path is zero padded by adding four zeros at the back of the signal. The multipath signal is zero padded by adding two zeros at the front and two at the end. The zero mean Gaussian noise for each antenna element is added and the noise variance is 0.01. The initial weights are assumed to be 1. Following cases are considered.

A. Case 1

Figure 2, 3 and 4 shows the array factor plots for LSCMA with number of elements \( N = 5 \), \( 8 \) and \( 10 \) for 06 iterations for inter-element separation \( d = 0.5\lambda \) respectively. From fig. 5 (combined plot of fig. 2, 3 and 4) it is clear that LSCMA generates peak in the desired direction user AOA 45° and places nulls in the undesired direction where interferer is located i.e., at -30°. Figure 5 shows that the number of side-lobes (SL) increases with \( N \) with a decrease in beam-width and increase in gain. The most optimized value for \( N = 8 \) with better gain and less number of SL levels (SLL). Figure 5 shows that the gain improves to 47.75 dB \(( N = 10)\) from 42.09 dB \(( N = 8)\), 33.22 dB \(( N = 5)\) and the level of SL degrades to 0.1 \(( N = 10)\) from 0.2 \(( N = 8)\), 0.3 \(( N = 5)\) and the beam-width decreases to 13° \(( N = 10)\) from 18° \(( N = 8)\), 30° \(( N = 5)\). Also, the number of SL increases to 7 \(( N = 10)\) from 6 \(( N = 8)\), 4 \(( N = 5)\). In terms of generating nulls in the direction of interferers, appreciable reduction in levels at -30° is observed.

B. Case 2

The variation of array factor for LSCMA with number of elements equal to \( N = 5 \), \( 8 \) and \( 10 \) for 06 iterations are drawn for different inter-element separation \( d = 0.25\lambda \) (figure 6, 7 and 8) and \( d = 0.125\lambda \) (figure 10, 11 and 12). Figure 9 (combined plot of Figure 6, 7 and 8) and 13 (combined plot of Figure 10, 11 and 12) shows that performance of LSCMA degrades as indicated by an increase in beam-width. More levels at interferer AOA -30° are observed. Thus inter-element spacing must be \( 0.5\lambda \) as can be concluded from Case 1 and 2.

Fig. 2. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 5 \) and \( d = 0.5\lambda \)

Fig. 3. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 8 \) and \( d = 0.5\lambda \)
Fig. 4. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 10 \) and \( d = 0.5\lambda \)

Fig. 5. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 5, 8, 10 \) and \( d = 0.5\lambda \)

Fig. 6. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 5 \) and \( d = 0.25\lambda \)

Fig. 7. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 8 \) and \( d = 0.25\lambda \)

Fig. 8. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 10 \) and \( d = 0.25\lambda \)

Fig. 9. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 5, 8, 10 \) and \( d = 0.25\lambda \)

Fig. 10. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 5 \) and \( d = 0.125\lambda \)

Fig. 11. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 8 \) and \( d = 0.125\lambda \)
In this paper, the optimization capabilities of LSCMA blind adaptive beam-forming algorithms are explored and it is found that for inter-element spacing of 0.5λ with 8 elements, the beam-width of 18° is achieved with a gain of 42.09 dB. The number of iterations required is 03. LSCMA does not require \( d(k) \) the reference signal and thus bandwidth can be saved. Thus, the most optimum values obtained for antenna array using LSCMA are \( N = 8 \) (no. of elements) and \( d = 0.5\lambda \) (inter-element spacing).

Fig. 12. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 10 \) and \( d = 0.125\lambda \)

Fig. 13. Array factor plot for LSCMA with user AOA 45° and interferer AOA at -30° for \( N = 5, 8, 10 \) and \( d = 0.125\lambda \)

IV. CONCLUSION

In this paper, the optimization capabilities of LSCMA blind adaptive beam-forming algorithms are explored and it is found that for inter-element spacing of 0.5λ with 8 elements, the beam-width of 18° is achieved with a gain of 42.09 dB. The number of iterations required is 03. LSCMA does not require \( d(k) \) the reference signal and thus bandwidth can be saved. Thus, the most optimum values obtained for antenna array using LSCMA are \( N = 8 \) (no. of elements) and \( d = 0.5\lambda \) (inter-element spacing).

REFERENCES


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