

# Heuristic Optimization Algorithms for Terrain Splitting and Mapping Problem

Nguyen Duc Thien, Le Hoang Son, Pier Luca Lanzi, and Pham Huy Thong

**Abstract**—Recently, several attempts have been made to creating 3D Geographical Information Systems on Web environment from DEM terrain data. However, most of them are facing the Terrain Splitting and Mapping problem which mainly caused by terrains' sizes and their query capabilities. This problem is a challenge when we want to make 'truly' 3D WebGIS systems in equivalent to what have been represented in 2D ones. So far, an algorithm has been presented by Le Hoang Son et al [15] namely as SESA which serves for DEM terrain splitting with minimal memory space in each processor of a computing system. However, this algorithm has some limitations such as computing time and strategies to find solutions. In this paper, we will propose two novel algorithms based on Genetic Algorithm and Particle Swarm Optimization for this problem. The proposed algorithms will be evaluated and compared with SESA algorithm to show their efficiencies.

**Index Terms**—Genetic Algorithms, Particle Swarm Optimization, SESA, TSM problem.

## I. INTRODUCTION

3D Geographical Information System on Web (3D WebGIS) is increasingly important to industrial applications. Some examples of it can be found such as Real Estate Information System [7], [9], [27], Earthquake Disaster Prevention and Mitigation [21], Tourism [8], [19], [24], [28], Traveling [18] and many other ones [1], [20], [25]. In such applications, 3D virtual interfaces modeling terrains or parts of them are provided together with some analysis tools designed for specific problems. The idea behind these 3D WebGIS applications is the capability to manage, control and make decision through a graphical interface with geo-reference supports. As such, more fees or costs can be saved due to 'better' decisions are made.

Digital Elevation Model (DEM) [3], [10], [16], [17], [22], [26] is the input of 3D WebGIS systems. DEM terrain data can be in gridded formats, triangulation irregular network (TIN) or contour lines [23]. The most terrain data source used by many GIS applications is gridded DEM. Generally, it is a matrix containing elevation values of all major points in a terrain. These elevation values reflect changes of a terrain in different locations. For example, the mountain area will have equally elevation values on the top of it and higher values than surface area's ones. An important parameter of DEM terrain is the distances between major points or resolutions. Basically, these numbers are equal and show the accuracy of

the terrain. Shorter distances increase the number of major points and hence the size of terrain as well. Such large terrains sometimes can not be displayed totally by Web browsers. Indeed, this problem is the first obstacle in deploying 3D WebGIS applications.

Another important limitation of current 3D WebGIS systems is the query capability. Because, DEM terrain contains topographic data only, therefore it is hard to specify which information can be drawn from an area. Without the query capability, we can not perform any analysis functions related to attribute information of the terrain. Indeed, this is the basic problem that should be solved absolutely.

Both limitations above are exactly stated in the *Terrain Splitting and Mapping* (TSM) problem [15]. This problem is very important in GIS and is the basis for further advance processing tools. Furthermore, it is described as one of some currently promising trends in GIS researches nowadays [11], [12], [13], [14].

In some recent works [15], the authors have proposed two algorithms to solve the TSM problem. Among them, the second one, SESA algorithm, was designed to split a large terrain into some small ones for parallel computing with smallest memory space in each processor of the computing system. However, as we may state in the next section, this algorithm has some limitations and therefore should be ameliorated efficiently.

In this paper, we will present two novel algorithms based on Genetic Algorithm [2] and Particle Swarm Optimization [6] for the TSM problem. Both algorithms are well-suited and tested to be better than SESA algorithm.

The remainder of this paper is organized as follows. Section 2 elaborates the problem. Overview about SESA method will be presented in Section 3. Two novel algorithms are shown in the two next sections. Section 6 presents some results from experiments. Finally, we will make conclusion and future works in the last section.

## II. THE PROBLEM

Assume that we have a DEM terrain and some polygons in 2D Polygonal Vector Data (2PVD). Our purpose is to split the original terrain following by these polygons and the number of processors  $k$  with smallest memory space in all processors. This problem is formulated as follows

$$J_1 = \sum_{i=1}^k SP_i \rightarrow \min \quad . \quad (1)$$

The constraints are

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$$\left\{ \begin{array}{l} |SP_i| \leq \alpha \times S_{DEM} \\ |SP_i - SP_j| \leq \varepsilon \times S_{DEM} \\ i = \overline{1, k}, j = \overline{1, k}, i \neq j \end{array} \right. , \quad (2)$$

Where  $SP_i$ ,  $i = \overline{1, k}$  are the areas of smallest rectangles containing all polygons in processor  $i$ .  $S_{DEM}$  is the area of original terrain. The parameter  $\alpha$  is the saving threshold. The last parameter  $\varepsilon$  is the difference of areas between two processors. Normally, its range falls into (0, 5).

### III. RELATED WORKS

As mentioned in previous section, the authors in [15] have proposed the SESA algorithms, the first and only method, to solve the above problem.

The main idea of this algorithm is to traverse all partitions dividing  $n$  elements into  $k$  blocks. For each partition, calculate its blocks' areas and check the constraints (2). If finding a suitable partition, stop the algorithm and output the results. Certainly, to reduce the number of traversed partitions, a pre-processing step should be carried out to arrange some elements into specific blocks. Details of this algorithm are summarized as follows.

1. Calculate the distance matrix  $D = [d_{ij}]_{k \times k}$  where  $d_{ij} = d(C_i, C_j)$  is the distance between polygon  $U_i$  and  $U_j$  in 2PVD,  $i = \overline{1, l}$ ,  $j = \overline{1, l}$  and  $i \neq j$ .
2. Based on the distance matrix  $D$ , find an unmarked polygons  $U_i$  and its closet unmarked polygon  $U_j$  in term of minimal distance and distance is smaller than  $0.25 * \sqrt{nC^2 + nR^2}$  until all polygons are reached.
3. Calculate the area of polygon  $U_i (S_i)$ ,  $U_j (S_j)$  and both  $U_i$  and  $U_j (S_{ij})$ .
4. Additive Condition: If  $S_i \geq 80\% S_{ij}$  or  $S_j \geq 80\% S_{ij}$  then we add polygons  $U_i$  and  $U_j$  into a processor.
5. Repeat from Step 2 to Step 4 for other unmarked polygons. The final result is a set of polygons:  $\langle \{U_i, U_j\}, U_h / i, j, h = \overline{1, k}; i \neq j \neq h \rangle (*)$
6. Use a parallel partitioning algorithm to divide the set (\*) into  $k$  blocks with  $k$  is the number of processors. In this case, they used the best parallel partitioning algorithm from Hoang Chi Thanh et al. [5].

7. For each received block  $i$ , calculate the area of all polygons in this block  $SP_i$ ,  $i = \overline{1, k}$ .
8. Check the constraints (2). If they are satisfied then stop the partitioning algorithm and perform the Step 6, 7 and 8 of 2OPS algorithm [15] for all current partitions. Otherwise, return to Step 6 to find another solutions.
9. In case of no partitions satisfying the original conditions, conclude that for given parameters  $\alpha$  and  $\varepsilon$ , there does not exist any solution for our problem. Therefore, if users want to find other solutions then they should adjust the parameters. For example,  $\alpha' = \alpha + 5\%$  and  $\varepsilon' = \varepsilon + 1\%$ . In this situation, return to Step 6 to find other solutions.

However, these are two limitations in this algorithm. First, the 'suitable' solution found by SESA is not optimal in many cases. In the other words, two parameters  $\alpha$  and  $\varepsilon$  are not the smallest ones. Because in the implementation of SESA, the authors [15] constrain the number of iteration steps to ensure the time condition. Therefore, an optimal solution which is not located in these iteration steps can be ignored. Although the main objective of SESA is finding one good solution to reduce the total memory space in all processors, the problem should be increased to specifying the best solution in whole search area. Finally, the last weakness of SESA is its spending time on finding solution. After each number of partitions, the generator re-adjusts the parameters if it can not find any possible solution. This make the answer time is really long in case of no satisfied partition.

More details about this method and how to apply it to the TSM problem can be found in [15].

### IV. GENETIC ALGORITHM BASED TERRAIN SPLITTING ALGORITHM (GA-TSA)

Genetic algorithm (GA), originally proposed by Dr. John Holland from the University of Michigan in 1975 [2], [4], is a search heuristic that mimics the process of natural evolution. This heuristic is routinely used to generate useful solutions to optimization and search problems. Genetic algorithms belong to the larger class of evolutionary algorithms (EA), which generate solutions to optimization problems using techniques inspired by natural evolution, such as inheritance, mutation, selection, and crossover.

The whole algorithm based on Genetic Algorithm (GA-TSA) is described as follows.

#### Step 1: Population Initiation

Individual is encoded as a vector  $v = (v_1, v_2, \dots, v_n)$ , with  $n$  is the number of polygons and  $v_i \in \{1, 2, \dots, k\}$  is the index of part that polygon  $i^{th}$  belong to.

Example: In the figure below, a possible individual is

$$v = (1,1,2)$$

This means polygon  $U_1$  and  $U_2$  are assigned to processor  $P1$  and polygon  $U_3$  is assigned to processor  $P2$ .

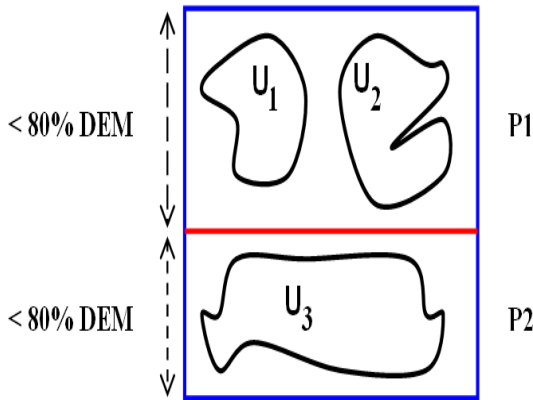


Fig 1. This terrain can be divided into two processors

The beginning population is initiated with  $P$  individuals ( $P$  is a designed parameter). Each individual is a vector with  $n$  components. The  $i^{th}$  component is an integer randomly generated within  $[1, k]$ .

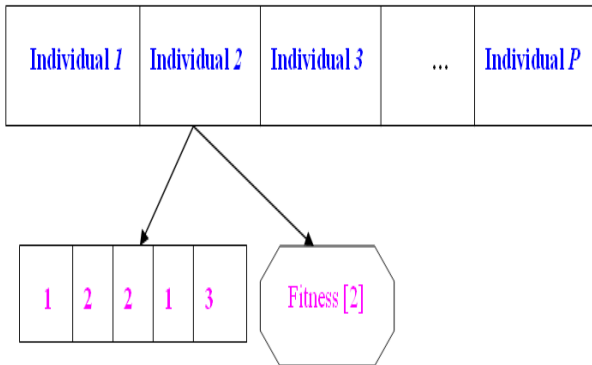


Fig 2. A population with  $n = 5$  and  $k = 3$

**Step 2: Calculate fitness values of all individuals in the current population by the following function**

$$f(v) = \frac{1}{\gamma_1 \times \max\{SP_i\} + \gamma_2 \times \max\{SP_i - SP_j\}} \quad , (3)$$

Where  $i = \overline{1, k}, j = \overline{1, k}, i \neq j$  and  $(\gamma_1, \gamma_2)$  are ratio constants. The meaning of these couple of parameters is to dynamically adjust the fitness function depending on the most important criteria. Because, it is possible that well fit individual is not always corresponding to a good partition. However, we expect that the satisfied partition is in well fit individuals.

**Step 3: Select the best-fit individuals for reproduction**

Use QuickSort algorithm to sort all individuals following by the ascent of their fitness values. Then, choose the

individuals in the range  $\left[1, \frac{P}{2}\right]$  to reproduce.

**Step 4: For each pair of individuals in the list of Step 3, perform Crossover and Mutation operations based on their probabilities to give birth to offspring. Outputted result of this step is a new population**

The Crossover operation contains two steps. First, use the Eliticism probability to copy some first individuals from parents to their child. This probability is calculated as

$$Eliticism = P * Eliticism\_Rate \quad , (4)$$

Where the *Eliticism\_Rate* is often 0.1.

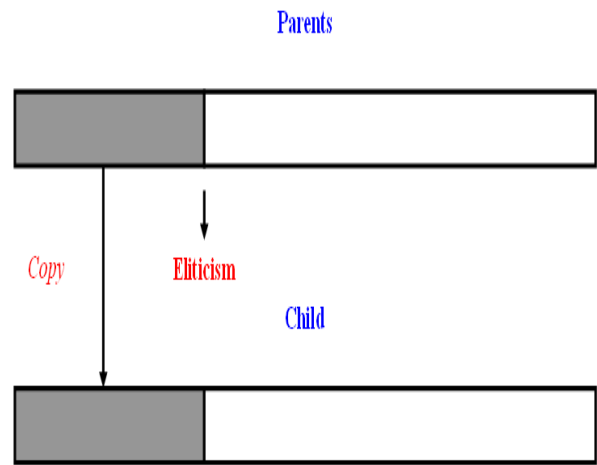


Fig 3. First step of Crossover operation

Second, use two randomly best-fit individuals in the previous step to create an offspring from the Eliticism position to the end of the Child. The offsprings are created by single-point probability between their selected parents.

$$Single\_Probability = Random(1, n) \quad . (5)$$

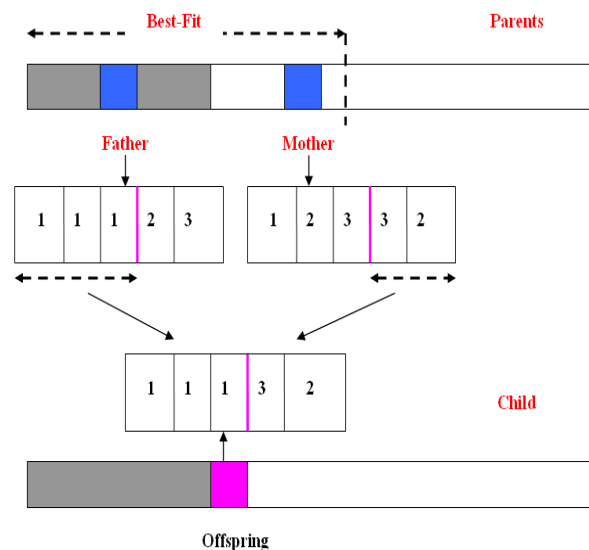


Fig 4. The Crossover operation

For each created offspring, if its mutation probability is less than a threshold ( $GA\_Mutation$ ) then we mutate it. The mutative individual is generated by replacing a random  $v_i$  by another random  $v_j$ ,  $i = \overline{1, n}$ ,  $j = \overline{1, n}$ .

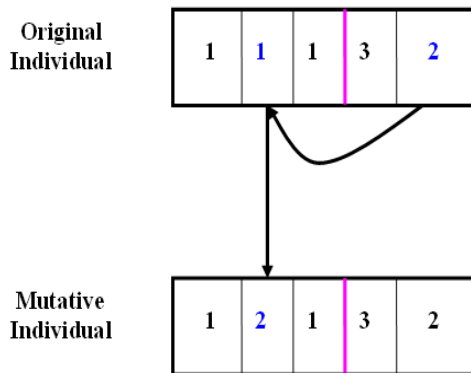


Fig 5. The Mutation operation

The Crossover and Mutation operations are continued to apply to other offsprings till the end of the Child.

**Step 5: Repeat from Step 2 to Step 4 until the number of iteration exceeds a pre-defined maximal iteration step ( $GA\_MaxIter$ )**

**Step 6: In case of at least an individual of current population satisfies the constraints (2), find the smallest parameter  $\alpha$  among all satisfied individuals. Then, perform the Step 6, 7 and 8 of 2OPS algorithm [15] for the optimal individual. Otherwise, no optimal solution is found.**

This algorithm will guarantee obtaining better results than SESA's ones. Later, we will check this consideration through Experiment.

#### V. PARTICLE SWARM OPTIMIZATION BASED TERRAIN SPLITTING ALGORITHM (PSO-TSA)

In this section, we try another method based on Swarm Optimization for our problem.

Particle swarm optimization (PSO) [6] is a population based stochastic optimization technique developed by Dr. Eberhart and Dr. Kennedy in 1995, inspired by social behavior of bird flocking or fish schooling. Generally, it is based on the principle: "The best strategy to find the food is to follow the bird which is nearest to it". Indeed, in PSO, each single solution is a "bird" or "particle" in the search space. All particles have fitness values which are evaluated by the fitness function to be optimized, and have velocities which direct the flying of the particles. The particles fly through the problem space by following the current optimum particles.

The basic idea of the new algorithm lies on the Seed Procedure. Basically,  $k$  seeds are evenly distributed in the space. Each seed represents for a number of polygons in 2PVD. Then, we calculate and check the constraints (2). If

these criteria are not met, use PSO algorithm to generate a new population until stopping condition is reached.

To specify whether a polygon  $i$  is represented by a seed  $j$ , we use the distance from the center of the smallest rectangle containing polygon  $i$  to this seed. If it is less than a given threshold then we add polygon  $i$  to seed  $j$ .

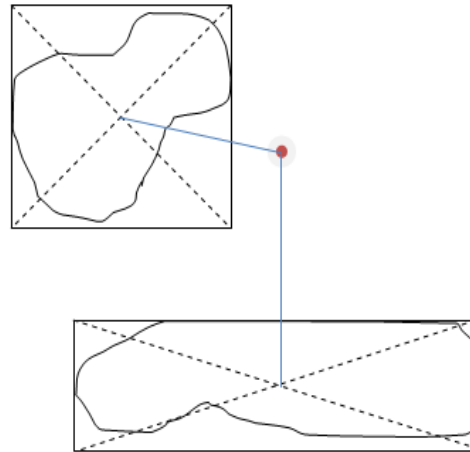


Fig 6. The distance from polygons to a seed point

However, it is possible that some seeds are too close. Therefore, a polygon may be represented by two or more seeds. Moreover, there exist seeds that do not represent for any polygon. These exceptions are depicted in Fig 7.

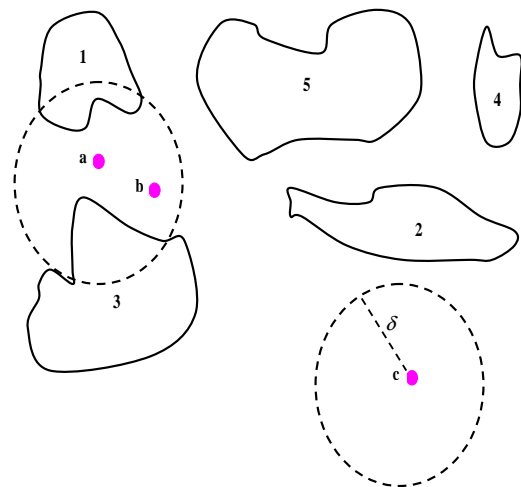


Fig 7. Some exceptions

Therefore, this representation may reduce the number of 'real' particles because some of them fall into exceptions. Instead, we perform some adjustments at the positions of seeds. Initially, we choose  $k$  random polygons in 2PVD and mark these centers as seeds. For the rests, they are assigned to the seed that is closet to them.

Details about the algorithm based on Particle Swarm Optimization (PSO-TSA) are presented below.

#### Step 1: Initialization

The beginning population is initiated with  $P$  particles where  $P$  is a designed parameter.

Each particle is a vector  $v = (v_1, v_2, \dots, v_k)$  where  $v_i$  is the seed point  $i^{th}$ ,  $i = \overline{1, k}$ . These seeds are centers of polygons randomly chosen from  $n$  polygons of 2PVD. Besides, we also initiate the velocities of these seeds to zeros.

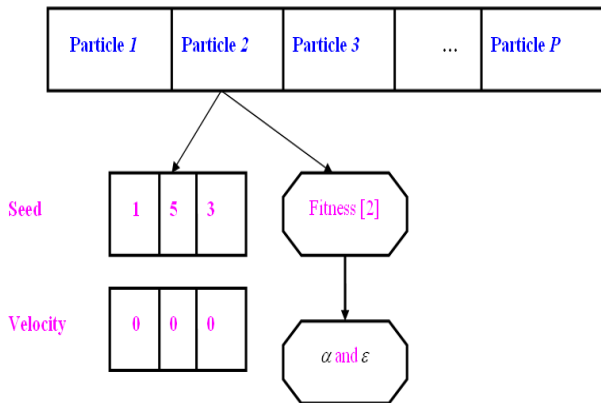


Fig 8. Beginning population

For the other polygons, they are assigned to the seed that is closet to them (Fig 9).

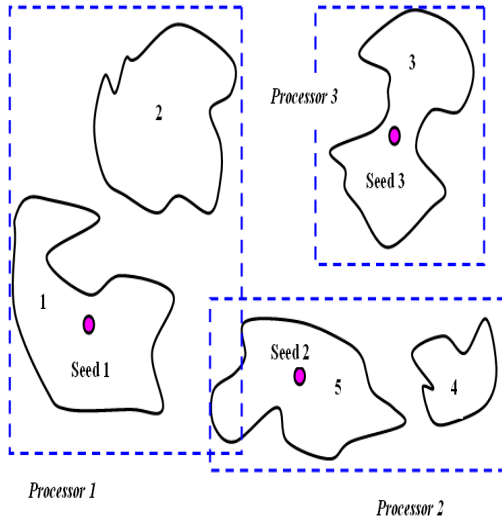


Fig 9. Assign remain polygons with  $n=5$  and  $k=3$

Similar process is applied for other particles (Fig 10).

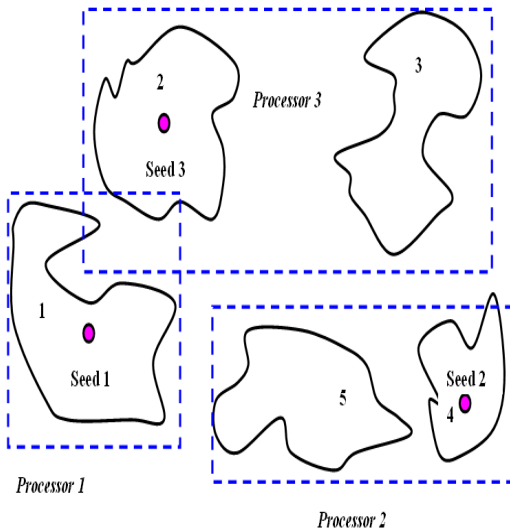


Fig 10. Another particle

**Step 2: Calculate fitness values of all particles**

In this case, we use the same fitness function (3). Then, the  $pBest$  value is specified. It is the best value that a particle has reached so far

- 2.1. For each particle  $p[i]$
- 2.2. If  $f(i) < pBest[i]$  then
- 2.3.  $pBest[i] = f(i)$
- 2.4. End If
- 2.5. End for

**Step 3: Calculate the global best value  $gBest$  among all particles. This is the best value in all iterations**

- 3.1. If  $gBest > pBest[i]$  then
- 3.2.  $gBest = pBest[i]$
- 3.3. End If

**Step 4: Calculate new velocities and positions of all seeds similar to the formulae in PSO algorithm [6]**

- 4.1. For each particle  $p[i]$
- 4.2. For each velocity  $j$
- 4.3.  $velocity[i][j] = c_1 * velocity[i][j] + c_2 * rand() * (seed[pBest][j] - seed[i][j]) + c_3 * rand() * (seed[gBest][j] - seed[i][j])$
- 4.4.  $seed[i][j] = seed[i][j] + velocity[i][j]$
- 4.5. End for
- 4.6. End for

In the formulae above,  $c_1$  is the ratio to keep the velocity intact,  $c_2$  is the ratio to change the velocity following by  $pBest$  value and  $c_3$  shows the influence level of  $gBest$  value to the velocity

$$c_1 + c_2 + c_3 = 1 \quad . (9)$$

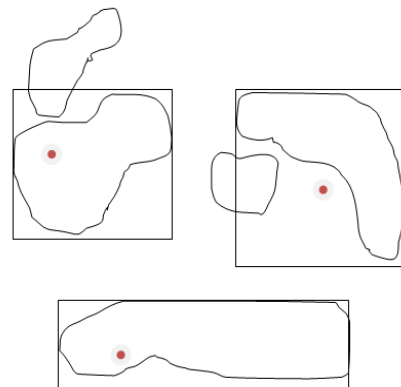


Fig 11. Seed moving in each particle

**Step 5: Repeat the whole process from Step 2 to Step 4 until the maximal iteration steps ( $PSO\_MaxIter$ ) is reached.**

**Step 6: In case of the particle holding  $gBest$  value satisfies the constraints (2), perform the Sep 6, 7, and 8 of 2OPS algorithm [15] for the optimal particle. Otherwise, conclude that no optimal solution is found.**

## VI. EXPERIMENTS

In this section, we have implemented the proposed algorithms GA-TSA and PSO-TSA in C programming language and executed them on a PC Core 2 Duo CPU 2 GHz and 1.96 GB of RAM. These algorithms were run against a large DEM terrain whose resolution is 25m and it contains more than 24 million elevation points. The 2PVD is taken from Towns containing 821 polygons (Fig 12). Both data are originated from Bolzano-Bolzen province, Italy in 2005.

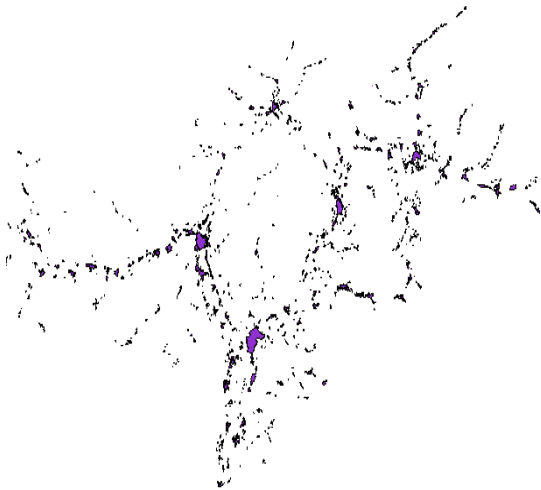


Fig 12. Towns Shape

Some parameters initialized in GA-TSA and PSO-TSA are

- GA population size:  $GA\_POPSIZE = 1000$
- GA maximal iterations:  $GA\_MaxIter = 100$
- Eliticism\_Rate:  $GA\_ELITRATE = 0.1$
- $GA\_MUTATIONRATE = 0.25$
- $(\gamma_1, \gamma_2) = (1,1)$
- PSO population size:  $PSO\_POPSIZE = 1000$
- PSO maximal iterations:  $PSO\_MaxIter = 100$
- $(c_1, c_2, c_3) = (0.2, 0.3, 0.5)$

First, we compare the parameter  $\alpha$  of GA-TSA, PSO-TSA and SESA algorithms when the number of polygons increases and the number of processors is four (Fig 13). Thence, we recognize that with maximal  $\mathcal{E} = 7\%$ , there is not much difference between results of SESA algorithm through different number of polygons. This can be explained as SESA is a greedy algorithm which returns an acceptable, first solution. Indeed, it is possible that a solution can be found in some first iterations of SESA through different

number of polygons. Consequently, these results seem unchanged. However, results of SESA algorithm are not optimal and far away from the ones of GA-TSA and PSO-TSA. The parameter  $\alpha$  found by two proposed algorithms ranges from 2.79% to 20.1% of the parameter found by SESA. Thus, it is obvious that we can save more memory space by using two novel algorithms.

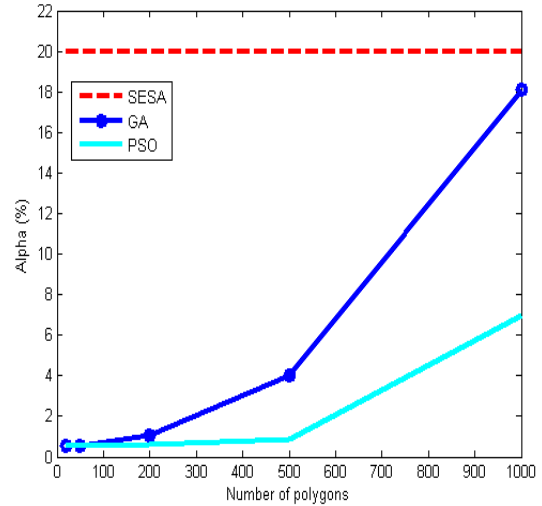


Fig 13. Compare the parameter  $\alpha$  (Alpha) of three algorithms

Moreover, PSO-TSA gives better results than GA-TSA does. Although, these two lines are quite close, however, some differences can be clearly seen when the number of polygons is larger. The average of difference between two algorithms changes from 0.002%, where the number of polygons smaller than 200, to 0.006% where the number of polygons smaller than 500. This difference can be higher if more polygons are added. Therefore, a conclusion can be drawn from this test: PSO-TSA brings smaller parameter  $\alpha$  than GA-TSA does.

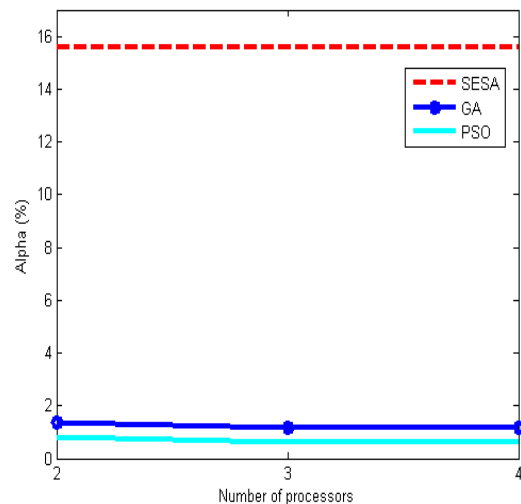


Fig 14. Compare the parameter  $\alpha$  (Alpha) by the number of processors

A similar result can be found at Fig 14 when the number of processors changes. However, the reducing ratio of two algorithms with respect to the SESA algorithm is only from 7.3% to 8.6%. Especially, more processors obtain less memory space in each processor. For example, when the

number of processors is doubled, the average reducing ratio of memory space in each processor is 12% to 25%. Certainly, PSO-TSA still reduces more memory space than GA-TSA does.

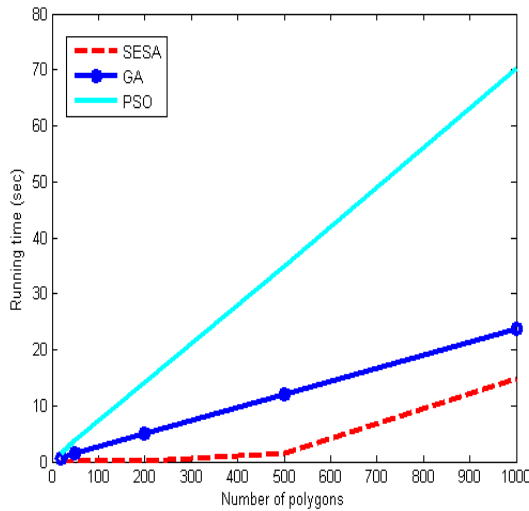


Fig 15. The running time of three algorithms

Fig 15 shows the running time of three algorithms following by the number of polygons. The test condition is similar to test 1 in Fig 13. From this, we can easily recognize that SESA is faster than GA-TSA (around 62%) and PSO-TSA (around 21%). The reason we have explained in the previous test. However, this result is quite relative because in some bad cases when the solution lies at the end of iteration steps, the running time of SESA is really long. This consideration was proved in the literature [15].

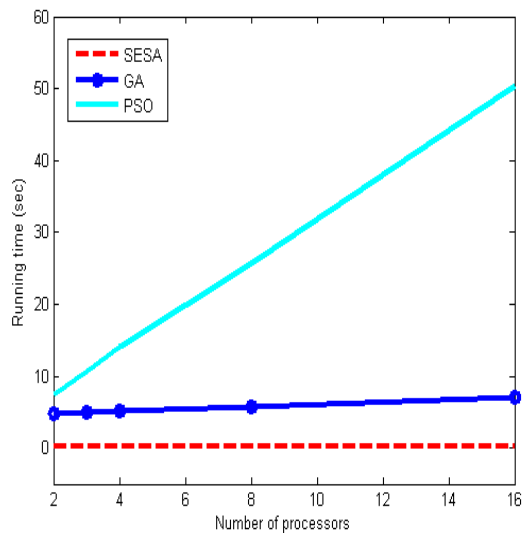


Fig 16. Compare the running time by the number of processors

The running time of PSO-TSA is 2.3 to 2.9 times slower than GA-TSA. Again, in Fig 16, we re-confirm this consideration. This test compare the running time of three algorithms following by the number of processors. The difference is manifested when the number of processors around 16. At that time, the running time of PSO-TSA is 7 times slower than GA-TSA and 323 times slower than SESA! Obviously, PSO-TSA can bring better parameter  $\alpha$ , but the cost we have to pay is the running time is too slow. Therefore,

a suitable number of processor is required to balance between result and running time. Throughout this test, we think four processors is a suitable answer (Fig 16).

## VII. CONCLUSION AND FUTURE WORKS

In this paper, we have investigated two heuristic optimization algorithms for the TSM problem. The first algorithm bases on Evolutionary Optimization, especially Genetic Algorithm (GA-TSA) and the second one PSO-TSA bases on swarm optimization. Both algorithms are implemented and tested through experiments to show the advantages in comparison with the SESA method [15]. Indeed, they are proved to be suitable for the TSM problem and be the basis to deploy further advance computing tools in 3D WebGIS.

In the future, we will look for some other stochastic optimization algorithms for the TSM problem. Moreover, some multi-objectives optimization problems in 3D WebGIS are also our targets.

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## APPENDIX

The source code and test dataset can be found at this address: <http://chpc.vnu.vn/gis/heuristic.rar>

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